

The massless box diagram with two legs on shell,
 $p_3^2 = p_4^2 = 0$, and two legs off shell, $p_1^2, p_2^2 \neq 0$

$$\begin{aligned}
B_{1100} &= i\pi^{d/2} \frac{\Gamma(a + \epsilon - 2)}{\prod \Gamma(a_l)} \\
&\times \int_0^\infty \dots \int_0^\infty \left(\prod_{l=1}^4 \alpha_l^{a_l-1} d\alpha_l \right) \delta \left(\sum_{l=1}^4 \alpha_l - 1 \right) \\
&\times (-s\alpha_1\alpha_3 - t\alpha_2\alpha_4 - p_1^2\alpha_1\alpha_2 - p_2^2\alpha_2\alpha_3 - i0)^{2-a-\epsilon}
\end{aligned}$$

Apply

$$\frac{1}{(X_1 + \dots + X_n)^\lambda} = \frac{1}{\Gamma(\lambda)} \frac{1}{(2\pi i)^{n-1}} \int_{-i\infty}^{+i\infty} \dots \int_{-i\infty}^{+i\infty} dz_2 \dots dz_n \prod_{i=2}^n X_i^{z_i}$$
$$\times X_1^{-\lambda - z_2 - \dots - z_n} \Gamma(\lambda + z_2 + \dots + z_n) \prod_{i=2}^n \Gamma(-z_i)$$

Separate terms with p_1^2 and p_2^2 , turn to new variables by

$$\alpha_1 = \eta_1 \xi_1, \quad \alpha_2 = \eta_1 (1 - \xi_1), \quad \alpha_3 = \eta_2 \xi_2, \quad \alpha_4 = \eta_2 (1 - \xi_2)$$

and evaluate integrals over parameters to obtain a three fold MB representation

$$\begin{aligned}
B_{1100} &= \frac{i\pi^{d/2}}{\Gamma(4 - 2\epsilon - a) \prod \Gamma(a_l)(-s)^{a+\epsilon-2}} \\
&\times \frac{1}{(2\pi i)^3} \int_{-i\infty}^{+i\infty} \int_{-i\infty}^{+i\infty} \int_{-i\infty}^{+i\infty} dz_2 dz_3 dz_4 \frac{(-p_1^2)^{z_2} (-p_2^2)^{z_3} (-t)^{z_4}}{(-s)^{z_2+z_3+z_4}} \\
&\times \Gamma(a + \epsilon - 2 + z_2 + z_3 + z_4) \Gamma(a_2 + z_2 + z_3 + z_4) \Gamma(a_4 + z_4) \\
&\times \Gamma(2 - \epsilon - a_{234} - z_3 - z_4) \Gamma(2 - \epsilon - a_{124} - z_2 - z_4) \\
&\times \Gamma(-z_2) \Gamma(-z_3) \Gamma(-z_4) .
\end{aligned}$$