

```

In[1]:= SetDirectory["c:/diskE/job2008/Zurich"];

(* http://www-ttp.particle.uni-karlsruhe.de/~asmirnov *)

In[2]:= << MB/MB.m;
<< MB/MBresolve.m

MB 1.1

by Michal Czakon

more info in hep-ph/0511200

last modified 06 Mar 08

MBresolve 1.0

by Alexander Smirnov

last modified 22 Oct 08

In[4]:= K2[a1_, a2_, a3_, a4_, a5_, a6_, a7_, a8_] :=
( xz1 Gamma[-z1] Gamma[a2+z1] Gamma[2-a5-a6-a7-ep-z1-z2]
Gamma[2-a1-a2-a8-ep+z2] Gamma[2-a4-a5-a7-ep-z1-z3]
Gamma[2-a2-a3-a8-ep+z3] Gamma[a7+z1-z4] Gamma[-2+a4+a5+a6+a7+ep+z1-z4]
Gamma[a8-z2-z3-z4] Gamma[-z1-z2-z3-z4] Gamma[-2+a1+a2+a3+a8+ep+z4]
Gamma[z2+z4] Gamma[z3+z4] Gamma[a5+z1+z2+z3+z4] ) /
(Gamma[a2] Gamma[a4] Gamma[a5] Gamma[a6] Gamma[a7] Gamma[4-a4-a5-a6-a7-2ep]
Gamma[4-a1-a2-a3-a8-2ep+z1-z4]
Gamma[a8-z1-z2-z3-z4] Gamma[a3+z2+z4] Gamma[a1+z3+z4])

In[5]:= B2 = K2[1, 1, 1, 1, 1, 1, 1, -1]

Out[5]:= ( xz1 Gamma[-z1] Gamma[1+z1] Gamma[-1-ep-z1-z2]
Gamma[1-ep+z2] Gamma[-1-ep-z1-z3] Gamma[1-ep+z3] Gamma[1+z1-z4]
Gamma[2+ep+z1-z4] Gamma[-1-z2-z3-z4] Gamma[-z1-z2-z3-z4]
Gamma[ep+z4] Gamma[z2+z4] Gamma[z3+z4] Gamma[1+z1+z2+z3+z4] ) /
(Gamma[-2ep] Gamma[2-2ep+z1-z4] Gamma[-1-z1-z2-z3-z4]
Gamma[1+z2+z4] Gamma[1+z3+z4])

In[6]:= MBOptimizedRules[B2, ep -> 0, {}, {ep}]

MBrules::norules : no rules could be found to regulate this integral

Out[6]:= {}

In[7]:= MBresolve[B2, ep]

CREATING RESIDUES LIST1.8281 seconds
FAILED TO RESOLVE

Out[7]:= False

In[10]:= B2 = K2[1, 1, 1, 1, 1, 1, 1, -1+y];

```

```
In[11]:= rul = MBOptimizedRules[B2, y → 0, {}, {y, ep}]
```

```
MBResidues::contour : contour starts and/or ends on a pole of Gamma[2 + 2 ep + y + z1]
```

```
MBResidues::contour : contour starts and/or ends on a pole of Gamma[1 + ep + y + z1]
```

```
MBResidues::contour : contour starts and/or ends on a pole of Gamma[2 ep + y - z3]
```

```
General::stop : Further output of MBResidues::contour will be suppressed during this calculation. >>
```

```
MBrules::norules : no rules could be found to regulate this integral
```

```
MBrules::norules : no rules could be found to regulate this integral
```

```
MBrules::norules : no rules could be found to regulate this integral
```

```
General::stop : Further output of MBrules::norules will be suppressed during this calculation. >>
```

```
Out[11]= {{y →  $\frac{55}{128}$ , ep →  $-\frac{107}{384}$ }, {z1 →  $-\frac{1}{6}$ , z2 →  $-\frac{73}{96}$ , z3 →  $-\frac{295}{384}$ , z4 →  $\frac{19}{24}$ }}
```

```
In[12]:= con1 = MBcontinue[B2, y → 0, rul];
```

```
Level 1
```

```
Taking -residue in z4 = -1 + y - z2 - z3
```

```
Level 2
```

```
Integral {1}
```

```
Taking +residue in z1 = -y
```

```
Taking -residue in z2 = -1 + y
```

```
Taking -residue in z3 = -1 + y
```

```
Level 3
```

```
Integral {1, 1}
```

```
Integral {1, 2}
```

```
Taking +residue in z1 = -y
```

```
Taking -residue in z3 = -1 + y
```

```
Integral {1, 3}
```

```
Taking +residue in z1 = -y
```

```
Level 4
```

```
Integral {1, 2, 1}
```

```
Integral {1, 2, 2}
```

```
Taking +residue in z1 = -y
```

```
Integral {1, 3, 1}
```

```
Level 5
```

```
Integral {1, 2, 2, 1}
```

```
9 integral(s) found
```

```
In[13]:= exp1 = MBexpand[con1, 1, {y, 0, 0}] // MBmerge;
```

```
In[14]:= con2 = Table[MBcontinue[exp1[[i, 1]], ep → 0, exp1[[i, 2]]], {i, Length[exp1]}] // MBmerge;
```

```
Level 1
```

```

1 integral(s) found
Level 1
1 integral(s) found
Level 1
Taking -residue in z2 = -1 - ep
Level 2
Integral {1}
2 integral(s) found
Level 1
Taking -residue in z3 = -1 - ep
Level 2
Integral {1}
2 integral(s) found
Level 1
Taking -residue in z2 = -1 - ep - z1
Level 2
Integral {1}
2 integral(s) found
Level 1
Taking -residue in z3 = -1 - ep - z1
Level 2
Integral {1}
2 integral(s) found
Level 1
Taking -residue in z2 = -1 - ep
Taking -residue in z3 = -1 - ep
Level 2
Integral {1}
Taking -residue in z3 = -1 - ep
Integral {2}
Level 3
Integral {1, 1}
4 integral(s) found
Level 1
Taking -residue in z2 = -1 - ep - z1
Taking -residue in z3 = -1 - ep - z1
Level 2

```

```
Integral {1}
Taking -residue in z3 = -1 - ep - z1
Integral {2}
Level 3
Integral {1, 1}
4 integral(s) found
Level 1
Taking -residue in z2 = -1 - ep - z1
Taking -residue in z3 = -1 - ep - z1
Level 2
Integral {1}
Taking -residue in z3 = -1 - ep - z1
Taking +residue in z4 = 1 + ep + z1
Integral {2}
Taking +residue in z4 = 1 + ep + z1
Level 3
Integral {1, 1}
Taking +residue in z4 = 1 + 2 ep + z1
...no contribution
Taking +residue in z4 = 1 + ep + z1
Integral {1, 2}
Integral {2, 1}
Level 4
Integral {1, 1, 1}
7 integral(s) found
```

In[15]:= **exp2 = MBexpand[con2, Exp[2 ep EulerGamma], {ep, 0, 0}] // MBmerge**

$$\text{Out[15]= } \left\{ \text{MBint} \left[ \frac{1}{1440 \text{ ep}^4} (3240 - 2820 \text{ ep}^2 \pi^2 + 31 \text{ ep}^4 \pi^4 + 9720 \text{ ep}^3 \text{ PolyGamma}[2, 1] - 480 \text{ ep} \text{ Log}[x] (6 - \text{ ep}^2 \pi^2 + 14 \text{ ep}^3 \text{ PolyGamma}[2, 1])) , \{ \{y \rightarrow 0, \text{ ep} \rightarrow 0\}, \{\} \} \right], \right. \\ \left. \text{MBint} \left[ -\frac{1}{\text{ ep}} 2 x^{z1} \text{ Gamma}[-z1]^2 \text{ Gamma}[z1] \text{ Gamma}[1+z1] \right. \right. \\ \left. \left. (\text{ Gamma}[-z1] \text{ Gamma}[1+z1] (-1 + \text{ ep} \text{ EulerGamma} + 4 \text{ ep} \text{ PolyGamma}[0, -z1] - 2 \text{ ep} \text{ PolyGamma}[0, z1] - \text{ ep} \text{ PolyGamma}[0, 1+z1]) + \text{ Gamma}[1-z1] \text{ Gamma}[z1] (3 - \text{ ep} \text{ EulerGamma} - 8 \text{ ep} \text{ PolyGamma}[0, -z1] + 2 \text{ ep} \text{ PolyGamma}[0, z1] + 5 \text{ ep} \text{ PolyGamma}[0, 1+z1])) , \right. \right. \\ \left. \left. \{ \{y \rightarrow 0, \text{ ep} \rightarrow 0\}, \{z1 \rightarrow -\frac{1}{6}\} \} \right], \text{MBint} \left[ \frac{1}{\text{ ep}} \text{ Gamma}[-1-z2]^2 \text{ Gamma}[1+z2]^2 \right. \right. \\ \left. \left. (-1 - 2 \text{ ep} \text{ EulerGamma} + \text{ ep} \text{ PolyGamma}[0, -1-z2] - 3 \text{ ep} \text{ PolyGamma}[0, 2+z2]) , \right. \right. \\ \left. \left. \{ \{y \rightarrow 0, \text{ ep} \rightarrow 0\}, \{z2 \rightarrow -\frac{73}{96}\} \} \right], \right. \\ \left. \text{MBint} \left[ \frac{1}{\text{ ep}} \text{ Gamma}[-1-z3]^2 \text{ Gamma}[1+z3]^2 \right. \right. \\ \left. \left. (-1 - 2 \text{ ep} \text{ EulerGamma} + \text{ ep} \text{ PolyGamma}[0, -1-z3] - 3 \text{ ep} \text{ PolyGamma}[0, 2+z3]) , \right. \right. \\ \left. \left. \{ \{y \rightarrow 0, \text{ ep} \rightarrow 0\}, \{z3 \rightarrow -\frac{295}{384}\} \} \right], \text{MBint} \left[ \frac{1}{\text{ Gamma}[2+z1+z2]} \right. \right. \\ \left. \left. 2 x^{z1} \text{ Gamma}[-z1] \text{ Gamma}[1+z1] \text{ Gamma}[-1-z2] \text{ Gamma}[1+z2] \text{ Gamma}[1+z1+z2] \right. \right. \\ \left. \left. (\text{ Gamma}[-z1] \text{ Gamma}[1+z1] \text{ Gamma}[-z1-z2] \text{ Gamma}[1+z1+z2] + \right. \right. \\ \left. \left. \text{ Gamma}[1-z1] \text{ Gamma}[z1] \text{ Gamma}[-1-z1-z2] \text{ Gamma}[2+z1+z2]) , \right. \right. \\ \left. \left. \{ \{y \rightarrow 0, \text{ ep} \rightarrow 0\}, \{z1 \rightarrow -\frac{1}{6}, z2 \rightarrow -\frac{73}{96}\} \} \right], \text{MBint} \left[ \frac{1}{\text{ Gamma}[2+z1+z3]} \right. \right. \\ \left. \left. 2 x^{z1} \text{ Gamma}[-z1] \text{ Gamma}[1+z1] \text{ Gamma}[-1-z3] \text{ Gamma}[1+z3] \text{ Gamma}[1+z1+z3] \right. \right. \\ \left. \left. (\text{ Gamma}[-z1] \text{ Gamma}[1+z1] \text{ Gamma}[-z1-z3] \text{ Gamma}[1+z1+z3] + \right. \right. \\ \left. \left. \text{ Gamma}[1-z1] \text{ Gamma}[z1] \text{ Gamma}[-1-z1-z3] \text{ Gamma}[2+z1+z3]) , \right. \right. \\ \left. \left. \{ \{y \rightarrow 0, \text{ ep} \rightarrow 0\}, \{z1 \rightarrow -\frac{1}{6}, z3 \rightarrow -\frac{295}{384}\} \} \right] \right\}$$

(\*\*\*\*\*)

In[17]:= **B2 = K2[1, 1, 1, 1, 1, 1, 1, -1 + y]**

$$\text{Out[17]= } \left( x^{z1} \text{ Gamma}[-z1] \text{ Gamma}[1+z1] \text{ Gamma}[-1-\text{ ep}-z1-z2] \right. \\ \left. \text{ Gamma}[1-\text{ ep}-y+z2] \text{ Gamma}[-1-\text{ ep}-z1-z3] \text{ Gamma}[1-\text{ ep}-y+z3] \text{ Gamma}[1+z1-z4] \right. \\ \left. \text{ Gamma}[2+\text{ ep}+z1-z4] \text{ Gamma}[-1+y-z2-z3-z4] \text{ Gamma}[-z1-z2-z3-z4] \right. \\ \left. \text{ Gamma}[\text{ ep}+y+z4] \text{ Gamma}[z2+z4] \text{ Gamma}[z3+z4] \text{ Gamma}[1+z1+z2+z3+z4] \right) / \\ \left( \text{ Gamma}[-2 \text{ ep}] \text{ Gamma}[2-2 \text{ ep}-y+z1-z4] \text{ Gamma}[-1+y-z1-z2-z3-z4] \right. \\ \left. \text{ Gamma}[1+z2+z4] \text{ Gamma}[1+z3+z4] \right)$$

In[19]:= **res1 = MBresolve[B2, {ep → 0, y → 0}]**

CREATING RESIDUES LIST.....3.8125 seconds

EVALUATING RESIDUES.....0.4375 seconds

$$\text{Out[19]= } \left\{ \text{MBint} \left[ \frac{4 \text{ EulerGamma}^2 x^{-2 \text{ ep}-y} \text{ Gamma}[-\text{ ep}]^2 \text{ Gamma}[1+\text{ ep}] \text{ Gamma}[1+2 \text{ ep}]}{\text{ Gamma}[1-\text{ ep}]} + \right. \right. \\ \left. \frac{2 \text{ EulerGamma} x^{-2 \text{ ep}-y} \text{ Gamma}[-\text{ ep}]^2 \text{ Gamma}[1+\text{ ep}] \text{ Gamma}[1+2 \text{ ep}] \text{ Log}[x]}{\text{ Gamma}[1-\text{ ep}]} + \frac{1}{\text{ Gamma}[1-\text{ ep}]} \right. \\ \left. \frac{2 \text{ EulerGamma} x^{-2 \text{ ep}-y} \text{ Gamma}[-\text{ ep}]^2 \text{ Gamma}[1+\text{ ep}] \text{ Gamma}[1+2 \text{ ep}] \text{ PolyGamma}[0, -2 \text{ ep}]}{\text{ Gamma}[1-\text{ ep}]} + \right. \\ \left. \frac{1}{\text{ Gamma}[1-\text{ ep}]} 2 \text{ EulerGamma} x^{-2 \text{ ep}-y} \text{ Gamma}[-\text{ ep}]^2 \text{ Gamma}[1+\text{ ep}] \text{ Gamma}[1+2 \text{ ep}] \right. \\ \left. \text{ PolyGamma}[0, -\text{ ep}] - \frac{1}{\text{ Gamma}[1-\text{ ep}]} 2 \text{ EulerGamma} x^{-2 \text{ ep}-y} \text{ Gamma}[-\text{ ep}]^2 \right\}$$

$$\begin{aligned}
& \Gamma[1 + \epsilon p] \Gamma[1 + 2 \epsilon p] \text{PolyGamma}[0, 1 + 2 \epsilon p] + \frac{1}{\Gamma[1 - \epsilon p]} \\
& \frac{2 \text{EulerGamma} x^{-2 \epsilon p - y} \Gamma[-\epsilon p]^2 \Gamma[1 + \epsilon p] \Gamma[1 + 2 \epsilon p] \text{PolyGamma}[0, 1 - 2 \epsilon p - y] +}{\Gamma[1 - \epsilon p]} \\
& \frac{x^{-2 \epsilon p - y} \Gamma[-\epsilon p]^2 \Gamma[1 + \epsilon p] \Gamma[1 + 2 \epsilon p] \text{PolyGamma}[1, 1 - \epsilon p]}{\Gamma[1 - \epsilon p]} + \\
& \frac{1}{2} \left( -\frac{1}{\Gamma[1 - \epsilon p]} \Gamma[-\epsilon p]^2 \Gamma[1 + \epsilon p] \Gamma[1 + 2 \epsilon p] \right. \\
& \left. \left( -2 \left( 2 \text{EulerGamma}^2 + 2 \left( \text{EulerGamma}^2 + \frac{\pi^2}{6} \right) \right) x^{-2 \epsilon p - y} - 8 \text{EulerGamma} x^{-2 \epsilon p - y} \text{Log}[x] - \right. \right. \\
& \left. \left. 2 x^{-2 \epsilon p - y} \text{Log}[x]^2 \right) - 2 \left( -\frac{4 \text{EulerGamma} x^{-2 \epsilon p - y} \Gamma[-\epsilon p]^2 \Gamma[1 + \epsilon p]}{\Gamma[1 - \epsilon p]} - \right. \right. \\
& \left. \left. \frac{2 x^{-2 \epsilon p - y} \Gamma[-\epsilon p]^2 \Gamma[1 + \epsilon p] \text{Log}[x]}{\Gamma[1 - \epsilon p]} \right) \right) (-\text{EulerGamma} \Gamma[1 + 2 \epsilon p] + \\
& \Gamma[1 + 2 \epsilon p] \text{PolyGamma}[0, -2 \epsilon p] + \Gamma[1 + 2 \epsilon p] \text{PolyGamma}[0, -\epsilon p] - \\
& \Gamma[1 + 2 \epsilon p] \text{PolyGamma}[0, 1 + 2 \epsilon p] + \Gamma[1 + 2 \epsilon p] \text{PolyGamma}[0, 1 - 2 \epsilon p - y]) + \\
& \frac{1}{\Gamma[1 - \epsilon p]} 2 x^{-2 \epsilon p - y} \Gamma[-\epsilon p]^2 \Gamma[1 + \epsilon p] \\
& \left( 2 \Gamma[1 + 2 \epsilon p] \text{PolyGamma}[0, -2 \epsilon p] \text{PolyGamma}[0, -\epsilon p] + \right. \\
& 2 (\Gamma[1 + 2 \epsilon p] \text{PolyGamma}[0, -2 \epsilon p] + \Gamma[1 + 2 \epsilon p] \text{PolyGamma}[0, -\epsilon p]) \\
& (-\text{EulerGamma} - \text{PolyGamma}[0, 1 + 2 \epsilon p] + \text{PolyGamma}[0, 1 - 2 \epsilon p - y]) + \\
& \Gamma[1 + 2 \epsilon p] (\text{PolyGamma}[0, -2 \epsilon p]^2 + \text{PolyGamma}[1, -2 \epsilon p]) + \\
& \Gamma[1 + 2 \epsilon p] (\text{PolyGamma}[0, -\epsilon p]^2 + \text{PolyGamma}[1, -\epsilon p]) + \Gamma[1 + 2 \epsilon p] \\
& \left. \left( -\frac{\pi^2}{3} + \text{PolyGamma}[0, 1 + 2 \epsilon p]^2 - 2 \text{PolyGamma}[0, 1 + 2 \epsilon p] \text{PolyGamma}[0, 1 - 2 \epsilon p - y] + \right. \right. \\
& \left. \left. \text{PolyGamma}[0, 1 - 2 \epsilon p - y]^2 - 2 \text{EulerGamma} (-\text{PolyGamma}[0, 1 + 2 \epsilon p] + \text{PolyGamma}[0, 1 - 2 \epsilon p - y]) + \text{PolyGamma}[1, 1 + 2 \epsilon p] + \text{PolyGamma}[1, 1 - 2 \epsilon p - y] \right) \right), \\
& \{ \{ \epsilon p \rightarrow 0 \}, \{ \} \} \}, \text{MBInt} \left[ - (2 \text{EulerGamma} x^{-1+z^4} \Gamma[-\epsilon p] \Gamma[1 + \epsilon p] \Gamma[2 - y - z^4] \right. \\
& \left. \Gamma[1 - 2 \epsilon p - y - z^4]^2 \Gamma[z^4] \Gamma[-1 + y + z^4] \Gamma[-1 + \epsilon p + y + z^4]) / \right. \\
& \left. (\Gamma[1 - \epsilon p] \Gamma[-2 \epsilon p] \Gamma[1 - 2 \epsilon p - y]) + \right. \\
& \left. (x^{-1+z^4} \Gamma[-\epsilon p] \Gamma[1 + \epsilon p] \Gamma[2 - y - z^4] \Gamma[1 - 2 \epsilon p - y - z^4]^2 \right. \\
& \left. \Gamma[z^4] \Gamma[-1 + y + z^4] \Gamma[-1 + \epsilon p + y + z^4] \text{PolyGamma}[0, 1 - \epsilon p]) / \right. \\
& \left. (\Gamma[1 - \epsilon p] \Gamma[-2 \epsilon p] \Gamma[1 - 2 \epsilon p - y]) - \right. \\
& \left. (x^{-1+z^4} \Gamma[-\epsilon p] \Gamma[1 + \epsilon p] \Gamma[2 - y - z^4] \Gamma[1 - 2 \epsilon p - y - z^4]^2 \right. \\
& \left. \Gamma[z^4] \Gamma[-1 + y + z^4] \Gamma[-1 + \epsilon p + y + z^4] \text{PolyGamma}[0, -\epsilon p]) / \right. \\
& \left. (\Gamma[1 - \epsilon p] \Gamma[-2 \epsilon p] \Gamma[1 - 2 \epsilon p - y]) - \right. \\
& \left. (2 x^{-1+z^4} \Gamma[-\epsilon p] \Gamma[1 + \epsilon p] \Gamma[2 - y - z^4] \Gamma[1 - 2 \epsilon p - y - z^4]^2 \Gamma[z^4] \right. \\
& \left. \Gamma[-1 + y + z^4] \Gamma[-1 + \epsilon p + y + z^4] \text{PolyGamma}[0, 1 - 2 \epsilon p - y - z^4]) / \right. \\
& \left. (\Gamma[1 - \epsilon p] \Gamma[-2 \epsilon p] \Gamma[1 - 2 \epsilon p - y]) + \right. \\
& \left. (x^{-1+z^4} \Gamma[-\epsilon p] \Gamma[1 + \epsilon p] \Gamma[2 - y - z^4] \Gamma[1 - 2 \epsilon p - y - z^4]^2 \Gamma[z^4] \right. \\
& \left. \Gamma[-1 + y + z^4] \Gamma[-1 + \epsilon p + y + z^4] \text{PolyGamma}[0, -1 + \epsilon p + y + z^4]) / \right. \\
& \left. (\Gamma[1 - \epsilon p] \Gamma[-2 \epsilon p] \Gamma[1 - 2 \epsilon p - y]) - \right. \\
& \left. (x^{-1+z^4} \Gamma[-\epsilon p] \Gamma[1 + \epsilon p] \Gamma[2 - y - z^4] \Gamma[1 - 2 \epsilon p - y - z^4]^2 \right. \\
& \left. \Gamma[z^4] \Gamma[-1 + y + z^4] \Gamma[-1 + \epsilon p + y + z^4] \text{PolyGamma}[0, \epsilon p + y + z^4]) / \right. \\
& \left. (\Gamma[1 - \epsilon p] \Gamma[-2 \epsilon p] \Gamma[1 - 2 \epsilon p - y]) \right], \{ \{ \epsilon p \rightarrow 0 \}, \{ z^4 \rightarrow 1.18859 \} \} \}, \\
& \text{MBInt} \left[ - (2 \text{EulerGamma} x^{-1+z^4} \Gamma[-\epsilon p] \Gamma[1 + \epsilon p] \Gamma[2 - y - z^4] \right.
\end{aligned}$$

$$\begin{aligned}
& \frac{\Gamma[1 - 2 \text{ep} - y - z4]^2 \Gamma[z4] \Gamma[-1 + y + z4] \Gamma[-1 + \text{ep} + y + z4]}{(\Gamma[1 - \text{ep}] \Gamma[-2 \text{ep}] \Gamma[1 - 2 \text{ep} - y]) +} \\
& \left( x^{-1+z4} \Gamma[-\text{ep}] \Gamma[1 + \text{ep}] \Gamma[2 - y - z4] \Gamma[1 - 2 \text{ep} - y - z4]^2 \right. \\
& \quad \left. \Gamma[z4] \Gamma[-1 + y + z4] \Gamma[-1 + \text{ep} + y + z4] \text{PolyGamma}[0, 1 - \text{ep}] \right) / \\
& (\Gamma[1 - \text{ep}] \Gamma[-2 \text{ep}] \Gamma[1 - 2 \text{ep} - y]) - \\
& \left( x^{-1+z4} \Gamma[-\text{ep}] \Gamma[1 + \text{ep}] \Gamma[2 - y - z4] \Gamma[1 - 2 \text{ep} - y - z4]^2 \right. \\
& \quad \left. \Gamma[z4] \Gamma[-1 + y + z4] \Gamma[-1 + \text{ep} + y + z4] \text{PolyGamma}[0, -\text{ep}] \right) / \\
& (\Gamma[1 - \text{ep}] \Gamma[-2 \text{ep}] \Gamma[1 - 2 \text{ep} - y]) - \\
& \left( 2 x^{-1+z4} \Gamma[-\text{ep}] \Gamma[1 + \text{ep}] \Gamma[2 - y - z4] \Gamma[1 - 2 \text{ep} - y - z4]^2 \Gamma[z4] \right. \\
& \quad \left. \Gamma[-1 + y + z4] \Gamma[-1 + \text{ep} + y + z4] \text{PolyGamma}[0, 1 - 2 \text{ep} - y - z4] \right) / \\
& (\Gamma[1 - \text{ep}] \Gamma[-2 \text{ep}] \Gamma[1 - 2 \text{ep} - y]) + \\
& \left( x^{-1+z4} \Gamma[-\text{ep}] \Gamma[1 + \text{ep}] \Gamma[2 - y - z4] \Gamma[1 - 2 \text{ep} - y - z4]^2 \Gamma[z4] \right. \\
& \quad \left. \Gamma[-1 + y + z4] \Gamma[-1 + \text{ep} + y + z4] \text{PolyGamma}[0, -1 + \text{ep} + y + z4] \right) / \\
& (\Gamma[1 - \text{ep}] \Gamma[-2 \text{ep}] \Gamma[1 - 2 \text{ep} - y]) - \\
& \left( x^{-1+z4} \Gamma[-\text{ep}] \Gamma[1 + \text{ep}] \Gamma[2 - y - z4] \Gamma[1 - 2 \text{ep} - y - z4]^2 \right. \\
& \quad \left. \Gamma[z4] \Gamma[-1 + y + z4] \Gamma[-1 + \text{ep} + y + z4] \text{PolyGamma}[0, \text{ep} + y + z4] \right) / \\
& (\Gamma[1 - \text{ep}] \Gamma[-2 \text{ep}] \Gamma[1 - 2 \text{ep} - y]), \{ \text{ep} \rightarrow 0 \}, \{ z4 \rightarrow 1.19354 \} \}, \\
\text{MBint} & \left[ \left( x^{-1+z4} \Gamma[1 + \text{ep}] \Gamma[-1 + y - z3] \Gamma[1 - \text{ep} - y + z3]^2 \Gamma[2 - y - z4] \right. \right. \\
& \quad \left. \Gamma[-\text{ep} - z3 - z4]^2 \Gamma[z4] \Gamma[-1 + y + z4] \Gamma[\text{ep} + y + z4] \Gamma[z3 + z4] \right) / \\
& (\Gamma[-2 \text{ep}] \Gamma[1 - 2 \text{ep} - y] \Gamma[y - z3] \Gamma[1 + z3 + z4]), \\
& \{ \text{ep} \rightarrow 0 \}, \{ z3 \rightarrow -1.07763, z4 \rightarrow 1.1663 \} \}, \\
\text{MBint} & \left[ \left( x^{-1+z4} \Gamma[-\text{ep}]^2 \Gamma[1 + \text{ep}] \Gamma[1 + 2 \text{ep}] \Gamma[1 - z4] \right. \right. \\
& \quad \left. \Gamma[1 - 2 \text{ep} - y - z4]^2 \Gamma[z4] \Gamma[\text{ep} + y + z4] \Gamma[-1 + 2 \text{ep} + y + z4] \right) / \\
& (\Gamma[1 - \text{ep}]^2 \Gamma[1 - 2 \text{ep} - y] \Gamma[2 \text{ep} + y]), \\
& \{ \text{ep} \rightarrow 0 \}, \{ z4 \rightarrow 0.649289 \} \}, \\
\text{MBint} & \left[ \left( x^{-1+z4} \Gamma[-\text{ep}] \Gamma[1 + \text{ep}] \Gamma[-1 + \text{ep} + y - z3] \Gamma[1 - \text{ep} - y + z3] \right. \right. \\
& \quad \Gamma[1 - z4] \Gamma[1 - 2 \text{ep} - y - z4] \Gamma[-\text{ep} - z3 - z4] \Gamma[1 + \text{ep} - z3 - z4] \\
& \quad \left. \Gamma[z4] \Gamma[\text{ep} + y + z4] \Gamma[z3 + z4] \Gamma[-\text{ep} + z3 + z4] \right) / \\
& (\Gamma[1 - \text{ep}] \Gamma[-2 \text{ep}] \Gamma[1 - 2 \text{ep} - y] \Gamma[\text{ep} + y - z3 - z4] \Gamma[1 + z3 + z4]), \\
& \{ \text{ep} \rightarrow 0 \}, \{ z3 \rightarrow -0.965164, z4 \rightarrow 0.969365 \} \}, \\
\text{MBint} & \left[ \left( x^{-1+z4} \Gamma[-\text{ep}] \Gamma[1 + \text{ep}] \Gamma[-1 + \text{ep} + y - z2] \Gamma[1 - \text{ep} - y + z2] \right. \right. \\
& \quad \Gamma[1 - z4] \Gamma[1 - 2 \text{ep} - y - z4] \Gamma[-\text{ep} - z2 - z4] \Gamma[1 + \text{ep} - z2 - z4] \\
& \quad \left. \Gamma[z4] \Gamma[\text{ep} + y + z4] \Gamma[z2 + z4] \Gamma[-\text{ep} + z2 + z4] \right) / \\
& (\Gamma[1 - \text{ep}] \Gamma[-2 \text{ep}] \Gamma[1 - 2 \text{ep} - y] \Gamma[\text{ep} + y - z2 - z4] \Gamma[1 + z2 + z4]), \\
& \{ \text{ep} \rightarrow 0 \}, \{ z2 \rightarrow -0.046298, z4 \rightarrow 0.940037 \} \}, \\
\text{MBint} & \left[ \left( x^{-1+z4} \Gamma[1 + \text{ep}] \Gamma[1 - \text{ep} - y + z2] \Gamma[1 - \text{ep} - y + z3] \Gamma[1 - z2 - z3 - 2 z4] \right. \right. \\
& \quad \Gamma[1 - z4] \Gamma[-\text{ep} - z2 - z4] \Gamma[-\text{ep} - z3 - z4] \Gamma[-1 + y - z2 - z3 - z4] \\
& \quad \left. \Gamma[z4] \Gamma[\text{ep} + y + z4] \Gamma[z2 + z4] \Gamma[z3 + z4] \Gamma[z2 + z3 + 2 z4] \right) / \\
& (\Gamma[-2 \text{ep}] \Gamma[1 - 2 \text{ep} - y] \Gamma[y - z2 - z3 - 2 z4] \Gamma[1 + z2 + z4] \Gamma[1 + z3 + z4]), \\
& \{ \text{ep} \rightarrow 0 \}, \{ z2 \rightarrow -0.195701, z3 \rightarrow -0.369613, z4 \rightarrow 0.372364 \} \}, \\
\text{MBint} & \left[ \frac{x^{-y} \Gamma[-2 \text{ep}] \Gamma[-\text{ep}]^2 \Gamma[2 \text{ep}] \Gamma[1 + 3 \text{ep}]}{\Gamma[1 - \text{ep}]}, \right. \\
& \left. \{ \text{ep} \rightarrow 0 \}, \{ \} \right], \\
\text{MBint} & \left[ \left( x^{-y} \Gamma[-\text{ep}] \Gamma[1 - y] \Gamma[1 - y - z4] \Gamma[1 - 2 \text{ep} - y - z4] \right. \right. \\
& \quad \Gamma[2 + \text{ep} - y - z4] \Gamma[-1 + y + z4] \Gamma[-1 + \text{ep} + y + z4] \right) / \\
& (\Gamma[1 - \text{ep}] \Gamma[2 - 2 \text{ep} - 2 y - z4]), \{ \text{ep} \rightarrow 0 \}, \{ z4 \rightarrow 1.19354 \} \}, \\
\text{MBint} & \left[ \left( x^{-y} \Gamma[-\text{ep}] \Gamma[1 - y] \Gamma[1 - y - z4] \Gamma[1 - 2 \text{ep} - y - z4] \right. \right. \\
& \quad \Gamma[2 + \text{ep} - y - z4] \Gamma[-1 + y + z4] \Gamma[-1 + \text{ep} + y + z4] \right) / \\
& (\Gamma[1 - \text{ep}] \Gamma[2 - 2 \text{ep} - 2 y - z4]), \{ \text{ep} \rightarrow 0 \}, \{ z4 \rightarrow 1.19354 \} \}, \\
\text{MBint} & \left[ \left( x^{-y} \Gamma[1 - y] \Gamma[-1 + y - z3] \Gamma[-1 - \text{ep} + y - z3] \right. \right. \\
& \quad \Gamma[1 - \text{ep} - y + z3] \Gamma[1 - y - z4] \Gamma[2 + \text{ep} - y - z4] \\
& \quad \left. \Gamma[-\text{ep} - z3 - z4] \Gamma[\text{ep} + y + z4] \Gamma[z3 + z4] \Gamma[-\text{ep} + z3 + z4] \right) / \\
& (\Gamma[-2 \text{ep}] \Gamma[y - z3] \Gamma[2 - 2 \text{ep} - 2 y - z4] \Gamma[1 + z3 + z4]),
\end{aligned}$$

```

{{ep → 0}, {z3 → -1.24579, z4 → 1.87263}}},
MBint [(x^z1 Gamma[-ep]^2 Gamma[1+ep] Gamma[1-y-z1] Gamma[-ep-y-z1]^2
Gamma[1+z1] Gamma[y+z1]^2 Gamma[1+ep+y+z1]) /
(Gamma[-2ep] Gamma[1-2ep+z1]), {{ep → 0}, {z1 → -0.377479}}],
MBint [(x^z1 Gamma[-ep] Gamma[1-y-z1] Gamma[-ep-y-z1] Gamma[1+z1]
Gamma[y+z1] Gamma[1-ep-y-z4] Gamma[1+z1-z4] Gamma[2+ep+z1-z4]
Gamma[-1+y+z4] Gamma[ep+y+z4] Gamma[-1-ep-z1+z4]) /
(Gamma[-2ep] Gamma[2-2ep-y+z1-z4] Gamma[y+z4]),
{{ep → 0}, {z1 → -0.731822, z4 → 0.76808}}],
MBint [(x^z1 Gamma[-ep] Gamma[1-y-z1] Gamma[-ep-y-z1] Gamma[1+z1]
Gamma[y+z1] Gamma[1-ep-y-z4] Gamma[1+z1-z4] Gamma[2+ep+z1-z4]
Gamma[-1+y+z4] Gamma[ep+y+z4] Gamma[-1-ep-z1+z4]) /
(Gamma[-2ep] Gamma[2-2ep-y+z1-z4] Gamma[y+z4]),
{{ep → 0}, {z1 → -0.547767, z4 → 0.832684}}],
MBint [(x^z1 Gamma[1-y-z1] Gamma[1+z1] Gamma[y+z1] Gamma[-1+y-z3]
Gamma[-1-ep-z1-z3] Gamma[1-ep-y+z3] Gamma[1+z1-z4] Gamma[2+ep+z1-z4]
Gamma[-ep-z3-z4] Gamma[ep+y+z4] Gamma[z3+z4] Gamma[-ep-y-z1+z3+z4]) /
(Gamma[-2ep] Gamma[y-z3] Gamma[2-2ep-y+z1-z4] Gamma[1+z3+z4]),
{{ep → 0}, {z1 → -0.515369, z3 → -0.80967, z4 → 0.760071}}],
MBint [(x^z1 Gamma[-z1] Gamma[1+z1] Gamma[-1-ep-z1-z2] Gamma[1-ep-y+z2]
Gamma[-1-ep-z1-z3] Gamma[1-ep-y+z3] Gamma[1+z1-z4]
Gamma[2+ep+z1-z4] Gamma[-1+y-z2-z3-z4] Gamma[-z1-z2-z3-z4]
Gamma[ep+y+z4] Gamma[z2+z4] Gamma[z3+z4] Gamma[1+z1+z2+z3+z4]) /
(Gamma[-2ep] Gamma[2-2ep-y+z1-z4] Gamma[-1+y-z1-z2-z3-z4]
Gamma[1+z2+z4] Gamma[1+z3+z4]),
{{ep → 0}, {z1 → -0.562672, z2 → -0.523479, z3 → -0.450782, z4 → 0.811527}}}]

```

```
In[20]:= res2 = MBpreselect[res1, {y, 0, 0}]
```

```
In[21]:= res3 = MBexpand[res2, 1, {y, 0, 0}]
```

```

Out[21]= {MBint [

$$\frac{4 \text{EulerGamma}^2 x^{-2 \text{ep}} \text{Gamma}[-\text{ep}]^2 \text{Gamma}[1+\text{ep}] \text{Gamma}[1+2 \text{ep}]}{\text{Gamma}[1-\text{ep}]} +$$


$$\frac{4 \text{EulerGamma} x^{-2 \text{ep}} \text{Gamma}[-\text{ep}]^2 \text{Gamma}[1+\text{ep}] \text{Gamma}[1+2 \text{ep}] \text{Log}[x]}{\text{Gamma}[1-\text{ep}]} +$$


$$\frac{x^{-2 \text{ep}} \text{Gamma}[-\text{ep}]^2 \text{Gamma}[1+\text{ep}] \text{Gamma}[1+2 \text{ep}] \text{Log}[x]^2}{\text{Gamma}[1-\text{ep}]} + \frac{1}{\text{Gamma}[1-\text{ep}]} +$$


$$\frac{4 \text{EulerGamma} x^{-2 \text{ep}} \text{Gamma}[-\text{ep}]^2 \text{Gamma}[1+\text{ep}] \text{Gamma}[1+2 \text{ep}] \text{PolyGamma}[0, 1-2 \text{ep}]}{\text{Gamma}[1-\text{ep}]} +$$


$$\frac{1}{\text{Gamma}[1-\text{ep}]} 2 x^{-2 \text{ep}} \text{Gamma}[-\text{ep}]^2 \text{Gamma}[1+\text{ep}] \text{Gamma}[1+2 \text{ep}] \text{Log}[x] \text{PolyGamma}[0, 1-2 \text{ep}] +$$


$$\frac{x^{-2 \text{ep}} \text{Gamma}[-\text{ep}]^2 \text{Gamma}[1+\text{ep}] \text{Gamma}[1+2 \text{ep}] \text{PolyGamma}[0, 1-2 \text{ep}]^2}{\text{Gamma}[1-\text{ep}]} + \frac{1}{\text{Gamma}[1-\text{ep}]} +$$


$$\frac{4 \text{EulerGamma} x^{-2 \text{ep}} \text{Gamma}[-\text{ep}]^2 \text{Gamma}[1+\text{ep}] \text{Gamma}[1+2 \text{ep}] \text{PolyGamma}[0, -2 \text{ep}]}{\text{Gamma}[1-\text{ep}]} +$$


$$\frac{1}{\text{Gamma}[1-\text{ep}]} 2 x^{-2 \text{ep}} \text{Gamma}[-\text{ep}]^2 \text{Gamma}[1+\text{ep}] \text{Gamma}[1+2 \text{ep}] \text{Log}[x] \text{PolyGamma}[0, -2 \text{ep}] +$$


$$\frac{1}{\text{Gamma}[1-\text{ep}]} 2 x^{-2 \text{ep}} \text{Gamma}[-\text{ep}]^2 \text{Gamma}[1+\text{ep}] \text{Gamma}[1+2 \text{ep}] \text{PolyGamma}[0, 1-2 \text{ep}] +$$


$$\text{PolyGamma}[0, -2 \text{ep}] + \frac{x^{-2 \text{ep}} \text{Gamma}[-\text{ep}]^2 \text{Gamma}[1+\text{ep}] \text{Gamma}[1+2 \text{ep}] \text{PolyGamma}[0, -2 \text{ep}]^2}{\text{Gamma}[1-\text{ep}]} +$$


$$\frac{1}{\text{Gamma}[1-\text{ep}]} 4 \text{EulerGamma} x^{-2 \text{ep}} \text{Gamma}[-\text{ep}]^2 \text{Gamma}[1+\text{ep}] \text{Gamma}[1+2 \text{ep}] \text{PolyGamma}[0, -\text{ep}] +$$


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$$\begin{aligned} & \left( \frac{\Gamma[-1 + \epsilon + z_4] \text{PolyGamma}[0, -\epsilon]}{\Gamma[1 - 2\epsilon] \Gamma[1 - \epsilon] \Gamma[-2\epsilon]} - \right. \\ & \left. \frac{(2 x^{-1+z_4} \Gamma[-\epsilon] \Gamma[1 + \epsilon] \Gamma[2 - z_4] \Gamma[1 - 2\epsilon - z_4]^2 \Gamma[-1 + z_4] \right. \\ & \left. \Gamma[z_4] \Gamma[-1 + \epsilon + z_4] \text{PolyGamma}[0, 1 - 2\epsilon - z_4])}{(\Gamma[1 - 2\epsilon] \Gamma[1 - \epsilon] \Gamma[-2\epsilon]) +} \right. \\ & \left. \frac{(x^{-1+z_4} \Gamma[-\epsilon] \Gamma[1 + \epsilon] \Gamma[2 - z_4] \Gamma[1 - 2\epsilon - z_4]^2 \right. \\ & \left. \Gamma[-1 + z_4] \Gamma[z_4] \Gamma[-1 + \epsilon + z_4] \text{PolyGamma}[0, -1 + \epsilon + z_4])}{(\Gamma[1 - 2\epsilon] \Gamma[1 - \epsilon] \Gamma[-2\epsilon]) - (x^{-1+z_4} \Gamma[-\epsilon] \Gamma[1 + \epsilon] \Gamma[2 - z_4] \right.} \\ & \left. \Gamma[1 - 2\epsilon - z_4]^2 \Gamma[-1 + z_4] \Gamma[z_4] \Gamma[-1 + \epsilon + z_4] \text{PolyGamma}[0, \epsilon + z_4])} \right) / \\ & \left. (\Gamma[1 - 2\epsilon] \Gamma[1 - \epsilon] \Gamma[-2\epsilon]), \{\{\epsilon \rightarrow 0\}, \{z_4 \rightarrow 1.19354\}\} \right], \\ \text{MBint} & \left[ \frac{(x^{-1+z_4} \Gamma[1 + \epsilon] \Gamma[-1 - z_3] \Gamma[1 - \epsilon + z_3]^2 \Gamma[2 - z_4] \right. \\ & \left. \Gamma[-\epsilon - z_3 - z_4]^2 \Gamma[-1 + z_4] \Gamma[z_4] \Gamma[\epsilon + z_4] \Gamma[z_3 + z_4])}{(\Gamma[1 - 2\epsilon] \Gamma[-2\epsilon] \Gamma[-z_3] \Gamma[1 + z_3 + z_4]),} \right. \\ & \left. \{\{\epsilon \rightarrow 0\}, \{z_3 \rightarrow -1.07763, z_4 \rightarrow 1.1663\}\} \right], \\ \text{MBint} & \left[ \frac{(x^{-1+z_4} \Gamma[-\epsilon]^2 \Gamma[1 + \epsilon] \Gamma[1 + 2\epsilon] \Gamma[1 - z_4] \right. \\ & \left. \Gamma[1 - 2\epsilon - z_4]^2 \Gamma[z_4] \Gamma[\epsilon + z_4] \Gamma[-1 + 2\epsilon + z_4])}{(\Gamma[1 - 2\epsilon] \Gamma[1 - \epsilon]^2 \Gamma[2\epsilon]),} \right. \\ & \left. \{\{\epsilon \rightarrow 0\}, \{z_4 \rightarrow 0.649289\}\} \right], \\ \text{MBint} & \left[ \frac{(x^{-1+z_4} \Gamma[-\epsilon] \Gamma[1 + \epsilon] \Gamma[-1 + \epsilon - z_3] \Gamma[1 - \epsilon + z_3] \right. \\ & \left. \Gamma[1 - z_4] \Gamma[1 - 2\epsilon - z_4] \Gamma[-\epsilon - z_3 - z_4] \Gamma[1 + \epsilon - z_3 - z_4] \right. \\ & \left. \Gamma[z_4] \Gamma[\epsilon + z_4] \Gamma[z_3 + z_4] \Gamma[-\epsilon + z_3 + z_4])}{(\Gamma[1 - 2\epsilon] \Gamma[1 - \epsilon] \Gamma[-2\epsilon] \Gamma[\epsilon - z_3 - z_4] \Gamma[1 + z_3 + z_4]),} \right. \\ & \left. \{\{\epsilon \rightarrow 0\}, \{z_3 \rightarrow -0.965164, z_4 \rightarrow 0.969365\}\} \right], \\ \text{MBint} & \left[ \frac{(x^{-1+z_4} \Gamma[-\epsilon] \Gamma[1 + \epsilon] \Gamma[-1 + \epsilon - z_2] \Gamma[1 - \epsilon + z_2] \right. \\ & \left. \Gamma[1 - z_4] \Gamma[1 - 2\epsilon - z_4] \Gamma[-\epsilon - z_2 - z_4] \Gamma[1 + \epsilon - z_2 - z_4] \right. \\ & \left. \Gamma[z_4] \Gamma[\epsilon + z_4] \Gamma[z_2 + z_4] \Gamma[-\epsilon + z_2 + z_4])}{(\Gamma[1 - 2\epsilon] \Gamma[1 - \epsilon] \Gamma[-2\epsilon] \Gamma[\epsilon - z_2 - z_4] \Gamma[1 + z_2 + z_4]),} \right. \\ & \left. \{\{\epsilon \rightarrow 0\}, \{z_2 \rightarrow -0.046298, z_4 \rightarrow 0.940037\}\} \right], \\ \text{MBint} & \left[ \frac{(x^{-1+z_4} \Gamma[1 + \epsilon] \Gamma[1 - \epsilon + z_2] \Gamma[1 - \epsilon + z_3] \Gamma[1 - z_2 - z_3 - 2 z_4] \right. \\ & \left. \Gamma[1 - z_4] \Gamma[-\epsilon - z_2 - z_4] \Gamma[-\epsilon - z_3 - z_4] \Gamma[-1 - z_2 - z_3 - z_4] \right. \\ & \left. \Gamma[z_4] \Gamma[\epsilon + z_4] \Gamma[z_2 + z_4] \Gamma[z_3 + z_4] \Gamma[z_2 + z_3 + 2 z_4])}{(\Gamma[1 - 2\epsilon] \Gamma[-2\epsilon] \Gamma[-z_2 - z_3 - 2 z_4] \Gamma[1 + z_2 + z_4] \Gamma[1 + z_3 + z_4]),} \right. \\ & \left. \{\{\epsilon \rightarrow 0\}, \{z_2 \rightarrow -0.195701, z_3 \rightarrow -0.369613, z_4 \rightarrow 0.372364\}\} \right], \\ \text{MBint} & \left[ \frac{\Gamma[-2\epsilon] \Gamma[-\epsilon]^2 \Gamma[2\epsilon] \Gamma[1 + 3\epsilon]}{\Gamma[1 - \epsilon]}, \{\{\epsilon \rightarrow 0\}, \{\}\} \right], \\ \text{MBint} & \left[ (\Gamma[-\epsilon] \Gamma[1 - z_4] \Gamma[1 - 2\epsilon - z_4] \Gamma[2 + \epsilon - z_4] \Gamma[-1 + z_4] \right. \\ & \left. \Gamma[-1 + \epsilon + z_4]) / (\Gamma[1 - \epsilon] \Gamma[2 - 2\epsilon - z_4]), \{\{\epsilon \rightarrow 0\}, \{z_4 \rightarrow 1.19354\}\} \right], \\ \text{MBint} & \left[ (\Gamma[-\epsilon] \Gamma[1 - z_4] \Gamma[1 - 2\epsilon - z_4] \Gamma[2 + \epsilon - z_4] \Gamma[-1 + z_4] \right. \\ & \left. \Gamma[-1 + \epsilon + z_4]) / (\Gamma[1 - \epsilon] \Gamma[2 - 2\epsilon - z_4]), \{\{\epsilon \rightarrow 0\}, \{z_4 \rightarrow 1.19354\}\} \right], \\ \text{MBint} & \left[ (\Gamma[-1 - z_3] \Gamma[-1 - \epsilon - z_3] \Gamma[1 - \epsilon + z_3] \Gamma[1 - z_4] \Gamma[2 + \epsilon - z_4] \right. \\ & \left. \Gamma[-\epsilon - z_3 - z_4] \Gamma[\epsilon + z_4] \Gamma[z_3 + z_4] \Gamma[-\epsilon + z_3 + z_4]) / \right. \\ & \left. (\Gamma[-2\epsilon] \Gamma[-z_3] \Gamma[2 - 2\epsilon - z_4] \Gamma[1 + z_3 + z_4]), \{\{\epsilon \rightarrow 0\}, \{z_3 \rightarrow -1.24579, z_4 \rightarrow 1.87263\}\} \right], \\ \text{MBint} & \left[ \frac{(x^{z_1} \Gamma[-\epsilon]^2 \Gamma[1 + \epsilon] \Gamma[1 - z_1] \Gamma[-\epsilon - z_1]^2 \Gamma[z_1]^2 \Gamma[1 + z_1] \right. \\ & \left. \Gamma[1 + \epsilon + z_1])}{(\Gamma[-2\epsilon] \Gamma[1 - 2\epsilon + z_1]),} \{\{\epsilon \rightarrow 0\}, \{z_1 \rightarrow -0.377479\}\} \right], \\ \text{MBint} & \left[ \frac{(x^{z_1} \Gamma[-\epsilon] \Gamma[1 - z_1] \Gamma[-\epsilon - z_1] \Gamma[z_1] \Gamma[1 + z_1] \right. \\ & \left. \Gamma[1 - \epsilon - z_4] \Gamma[1 + z_1 - z_4] \Gamma[2 + \epsilon + z_1 - z_4] \Gamma[-1 + z_4] \Gamma[\epsilon + z_4] \right. \\ & \left. \Gamma[-1 - \epsilon - z_1 + z_4])}{(\Gamma[-2\epsilon] \Gamma[2 - 2\epsilon + z_1 - z_4] \Gamma[z_4]),} \right. \\ & \left. \{\{\epsilon \rightarrow 0\}, \{z_1 \rightarrow -0.731822, z_4 \rightarrow 0.76808\}\} \right], \text{MBint} \left[ \right. \\ & \left. \frac{(x^{z_1} \Gamma[-\epsilon] \Gamma[1 - z_1] \Gamma[-\epsilon - z_1] \Gamma[z_1] \Gamma[1 + z_1] \Gamma[1 - \epsilon - z_4] \Gamma[1 + z_1 - z_4] \right. \\ & \left. \Gamma[2 + \epsilon + z_1 - z_4] \Gamma[-1 + z_4] \Gamma[\epsilon + z_4] \Gamma[-1 - \epsilon - z_1 + z_4])}{(\Gamma[-2\epsilon] \Gamma[2 - 2\epsilon + z_1 - z_4] \Gamma[z_4]),} \{\{\epsilon \rightarrow 0\}, \right. \\ & \left. \{z_1 \rightarrow -0.547767, z_4 \rightarrow 0.832684\}\} \right], \\ \text{MBint} & \left[ \frac{(x^{z_1} \Gamma[1 - z_1] \Gamma[z_1] \Gamma[1 + z_1] \Gamma[-1 - z_3] \Gamma[-1 - \epsilon - z_1 - z_3] \right. \\ & \left. \Gamma[1 - \epsilon + z_3] \Gamma[1 + z_1 - z_4] \Gamma[2 + \epsilon + z_1 - z_4]) \right. \end{aligned}$$

$$\frac{\Gamma[-\epsilon - z_3 - z_4] \Gamma[\epsilon + z_4] \Gamma[z_3 + z_4] \Gamma[-\epsilon - z_1 + z_3 + z_4]}{(\Gamma[-2\epsilon] \Gamma[-z_3] \Gamma[2 - 2\epsilon + z_1 - z_4] \Gamma[1 + z_3 + z_4])},$$

$$\{\{\epsilon \rightarrow 0\}, \{z_1 \rightarrow -0.515369, z_3 \rightarrow -0.80967, z_4 \rightarrow 0.760071\}\},$$

$$\text{MBint}\left[\left(x^{z_1} \Gamma[-z_1] \Gamma[1 + z_1] \Gamma[-1 - \epsilon - z_1 - z_2] \Gamma[1 - \epsilon + z_2] \Gamma[-1 - \epsilon - z_1 - z_3] \Gamma[1 - \epsilon + z_3] \Gamma[1 + z_1 - z_4] \Gamma[2 + \epsilon + z_1 - z_4] \Gamma[-1 - z_2 - z_3 - z_4] \Gamma[-z_1 - z_2 - z_3 - z_4] \Gamma[\epsilon + z_4] \Gamma[z_2 + z_4] \Gamma[z_3 + z_4] \Gamma[1 + z_1 + z_2 + z_3 + z_4]\right) / (\Gamma[-2\epsilon] \Gamma[2 - 2\epsilon + z_1 - z_4] \Gamma[-1 - z_1 - z_2 - z_3 - z_4] \Gamma[1 + z_2 + z_4] \Gamma[1 + z_3 + z_4])\right],$$

$$\{\{\epsilon \rightarrow 0\}, \{z_1 \rightarrow -0.562672, z_2 \rightarrow -0.523479, z_3 \rightarrow -0.450782, z_4 \rightarrow 0.811527\}\}$$

In[22]:= **res4 = MBpreselect[res3, { $\epsilon$ , 0, 0}]**

In[24]= `res5 = Simplify[MBexpand[res4, Exp[2 ep EulerGamma], {ep, 0, 0}]]`

Out[24]= 
$$\left\{ \text{MBint} \left[ \frac{5}{2 \text{ep}^4} - \frac{19 \pi^2}{12 \text{ep}^2} - \frac{13 \pi^4}{720} - \pi^2 \text{Log}[x]^2 + \frac{2 \text{Log}[x]^3}{3 \text{ep}} - \frac{\text{Log}[x]^4}{3} + \frac{47 \text{PolyGamma}[2, 1]}{6 \text{ep}} - \frac{\text{Log}[x] (6 - 7 \text{ep}^2 \pi^2 + 20 \text{ep}^3 \text{PolyGamma}[2, 1])}{3 \text{ep}^3}, \{\{\text{ep} \rightarrow 0\}, \{\}\} \right], \right.$$

$$\text{MBint} \left[ \frac{1}{\text{ep}} 2 x^{-1+z^4} \text{Gamma}[1-z^4]^2 \text{Gamma}[2-z^4] \text{Gamma}[-1+z^4]^2 \text{Gamma}[z^4] \right.$$

$$\left. (-1 + \text{ep EulerGamma} + 2 \text{ep PolyGamma}[0, 1-z^4] - \text{ep PolyGamma}[0, z^4]), \{\{\text{ep} \rightarrow 0\}, \{z^4 \rightarrow 1.18859\}\} \right], \text{MBint} \left[ \frac{1}{\text{ep}} 2 x^{-1+z^4} \text{Gamma}[1-z^4]^2 \text{Gamma}[2-z^4] \text{Gamma}[-1+z^4]^2 \right.$$

$$\left. \text{Gamma}[z^4] (-1 + \text{ep EulerGamma} + 2 \text{ep PolyGamma}[0, 1-z^4] - \text{ep PolyGamma}[0, z^4]), \{\{\text{ep} \rightarrow 0\}, \{z^4 \rightarrow 1.19354\}\} \right],$$

$$\text{MBint} \left[ -\frac{1}{\text{ep}} 2 x^{-1+z^4} \text{Gamma}[1-z^4]^3 \text{Gamma}[-1+z^4] \text{Gamma}[z^4]^2 (-1 + \text{ep EulerGamma} + 4 \text{ep PolyGamma}[0, 1-z^4] - 2 \text{ep PolyGamma}[0, -1+z^4] - \text{ep PolyGamma}[0, z^4]), \{\{\text{ep} \rightarrow 0\}, \{z^4 \rightarrow 0.649289\}\} \right], \text{MBint} \left[ \frac{1}{\text{Gamma}[1+z^3+z^4]} 2 x^{-1+z^4} \text{Gamma}[-1-z^3] \right.$$

$$\left. \text{Gamma}[1+z^3] \text{Gamma}[1-z^4]^2 \text{Gamma}[1-z^3-z^4] \text{Gamma}[z^4]^2 \text{Gamma}[z^3+z^4]^2, \{\{\text{ep} \rightarrow 0\}, \{z^3 \rightarrow -0.965164, z^4 \rightarrow 0.969365\}\} \right], \text{MBint} \left[ \frac{1}{\text{Gamma}[1+z^2+z^4]} 2 x^{-1+z^4} \text{Gamma}[-1-z^2] \right.$$

$$\left. \text{Gamma}[1+z^2] \text{Gamma}[1-z^4]^2 \text{Gamma}[1-z^2-z^4] \text{Gamma}[z^4]^2 \text{Gamma}[z^2+z^4]^2, \{\{\text{ep} \rightarrow 0\}, \{z^2 \rightarrow -0.046298, z^4 \rightarrow 0.940037\}\} \right],$$

$$\text{MBint} \left[ -\frac{120 + 180 \text{ep}^2 \pi^2 + 173 \text{ep}^4 \pi^4 + 520 \text{ep}^3 \text{PolyGamma}[2, 1]}{480 \text{ep}^4}, \{\{\text{ep} \rightarrow 0\}, \{\}\} \right],$$

$$\text{MBint} \left[ -\frac{1}{\text{ep}} \text{Gamma}[1-z^4]^2 \text{Gamma}[-1+z^4]^2 (1 + 2 \text{ep EulerGamma} - 2 \text{ep PolyGamma}[0, 1-z^4] + 3 \text{ep PolyGamma}[0, 2-z^4] + \text{ep PolyGamma}[0, -1+z^4]), \{\{\text{ep} \rightarrow 0\}, \{z^4 \rightarrow 1.19354\}\} \right],$$

$$\text{MBint} \left[ -\frac{1}{\text{ep}} \text{Gamma}[1-z^4]^2 \text{Gamma}[-1+z^4]^2 (1 + 2 \text{ep EulerGamma} - 2 \text{ep PolyGamma}[0, 1-z^4] + 3 \text{ep PolyGamma}[0, 2-z^4] + \text{ep PolyGamma}[0, -1+z^4]), \{\{\text{ep} \rightarrow 0\}, \{z^4 \rightarrow 1.19354\}\} \right],$$

$$\text{MBint} \left[ -\frac{1}{\text{ep}} 2 x^{z^1} \text{Gamma}[1-z^1] \text{Gamma}[-z^1]^2 \text{Gamma}[z^1]^2 \text{Gamma}[1+z^1] \right.$$

$$\left. (1 + \text{ep EulerGamma} - 2 \text{ep PolyGamma}[0, -z^1] + 3 \text{ep PolyGamma}[0, 1+z^1]), \{\{\text{ep} \rightarrow 0\}, \{z^1 \rightarrow -0.377479\}\} \right], \text{MBint} \left[ 2 x^{z^1} \text{Gamma}[1-z^1] \text{Gamma}[-z^1] \text{Gamma}[z^1] \right.$$

$$\left. \text{Gamma}[1+z^1] \text{Gamma}[1-z^4] \text{Gamma}[1+z^1-z^4] \text{Gamma}[-1+z^4] \text{Gamma}[-1-z^1+z^4], \{\{\text{ep} \rightarrow 0\}, \{z^1 \rightarrow -0.731822, z^4 \rightarrow 0.76808\}\} \right],$$

$$\text{MBint} \left[ 2 x^{z^1} \text{Gamma}[1-z^1] \text{Gamma}[-z^1] \text{Gamma}[z^1] \text{Gamma}[1+z^1] \text{Gamma}[1-z^4] \text{Gamma}[1+z^1-z^4] \right.$$

$$\left. \text{Gamma}[-1+z^4] \text{Gamma}[-1-z^1+z^4], \{\{\text{ep} \rightarrow 0\}, \{z^1 \rightarrow -0.547767, z^4 \rightarrow 0.832684\}\} \right] \left. \right\}$$