
The Spin Structure of the Nucleon as seen by HERMES

Benedikt Zihlmann

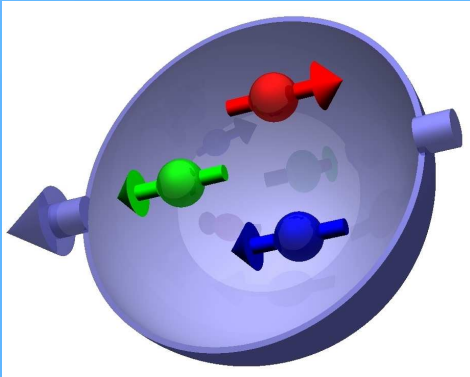
University of Gent

on behalf of the



collaboration

The Spin Structure of the Nucleon



Naive Parton Model:

$$\Delta u_v + \Delta d_v = 1$$
$$\implies \Delta u_v = \frac{4}{3}, \Delta d_v = \frac{-1}{3}$$

BUT

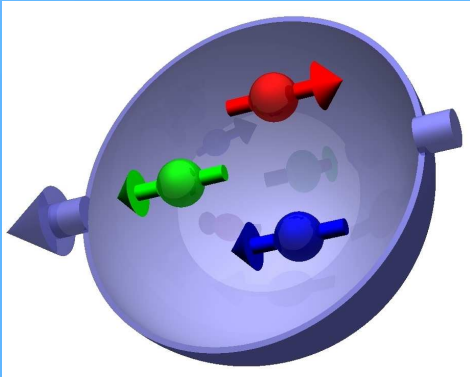
1988 EMC measured:

$$\Delta\Sigma = 0.123 \pm 0.013 \pm 0.019$$

\implies Spin Puzzle

$$\frac{1}{2} = \frac{1}{2}(\Delta u_v + \Delta d_v)$$

The Spin Structure of the Nucleon



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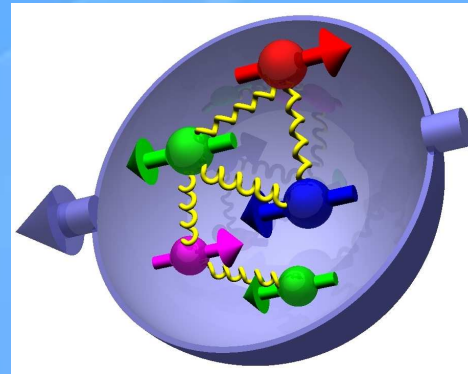
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from unpolarized data:

Gluons are important !

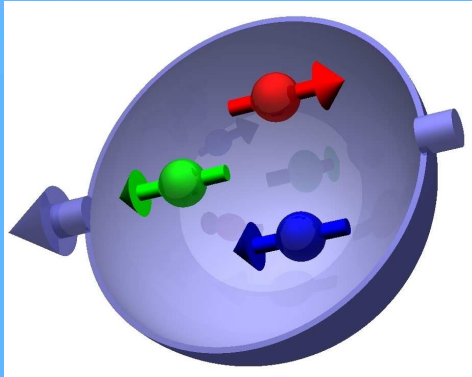
\implies sea quarks Δq_s

$\implies \Delta G$

$$\frac{1}{2} = \frac{1}{2} \left(\Delta u_v + \Delta d_v + \underbrace{\Delta q_s}_{\Delta u_s, \Delta d_s, \Delta \bar{u}, \Delta \bar{d}, \Delta s, \Delta \bar{s}} \right) + \Delta G$$

$\Delta u_s, \Delta d_s, \Delta \bar{u}, \Delta \bar{d}, \Delta s, \Delta \bar{s}$

The Spin Structure of the Nucleon



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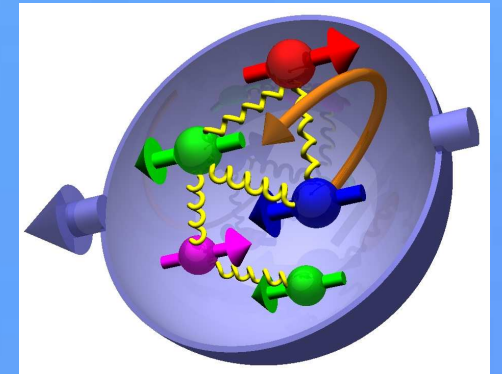
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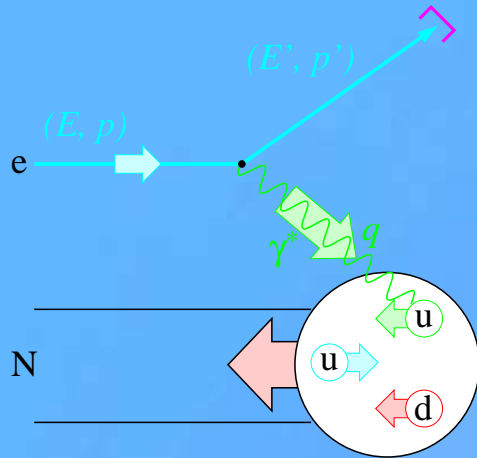


Full description of J_q & J_g
needs
orbital angular momentum

$$\frac{1}{2} = \frac{1}{2} \underbrace{(\Delta u_v + \Delta d_v + \Delta q_s)}_{\Delta\Sigma} + \mathbf{L}_q + (\Delta G + \mathbf{L}_g)$$

Deep Inelastic Scattering

Inclusive Scattering:



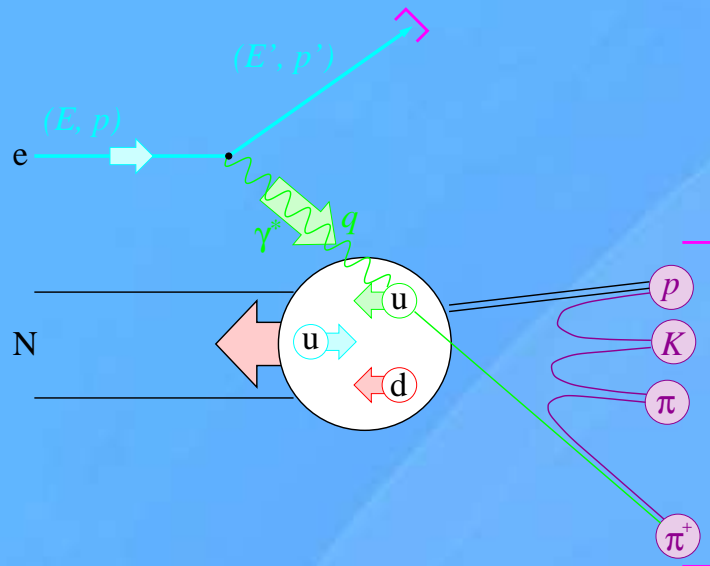
detect scattered lepton

$$Q^2 \stackrel{lab}{=} 4EE' \sin^2\left(\frac{\theta}{2}\right)$$

$$x \stackrel{lab}{=} \frac{Q^2}{2M\nu} \quad y \stackrel{lab}{=} \frac{\nu}{E} = \frac{\mathbf{p} \cdot \mathbf{q}}{\mathbf{p} \cdot \mathbf{k}}$$

Deep Inelastic Scattering

Semi-Inclusive Scattering:



detect scattered lepton and produced hadrons

$$Q^2 \stackrel{lab}{=} 4EE' \sin^2\left(\frac{\theta}{2}\right)$$

$$x \stackrel{lab}{=} \frac{Q^2}{2M\nu}$$

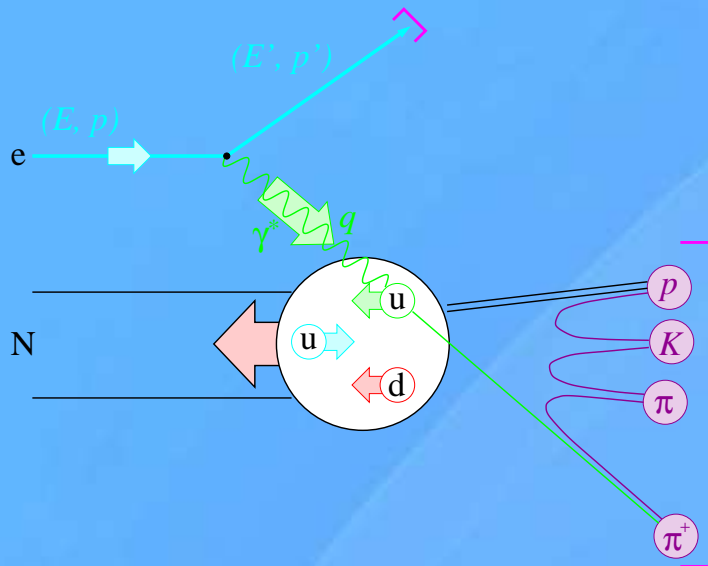
$$z \stackrel{lab}{=} \frac{E_h}{\nu}$$

$$y \stackrel{lab}{=} \frac{\nu}{E} = \frac{p \cdot q}{p \cdot k}$$

Deep Inelastic Scattering

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Cross Section:

$$\frac{d^2\sigma}{d\Omega dE^2} = \frac{\alpha^2 E'}{Q^2 E} L_{\mu\nu} W^{\mu\nu}$$

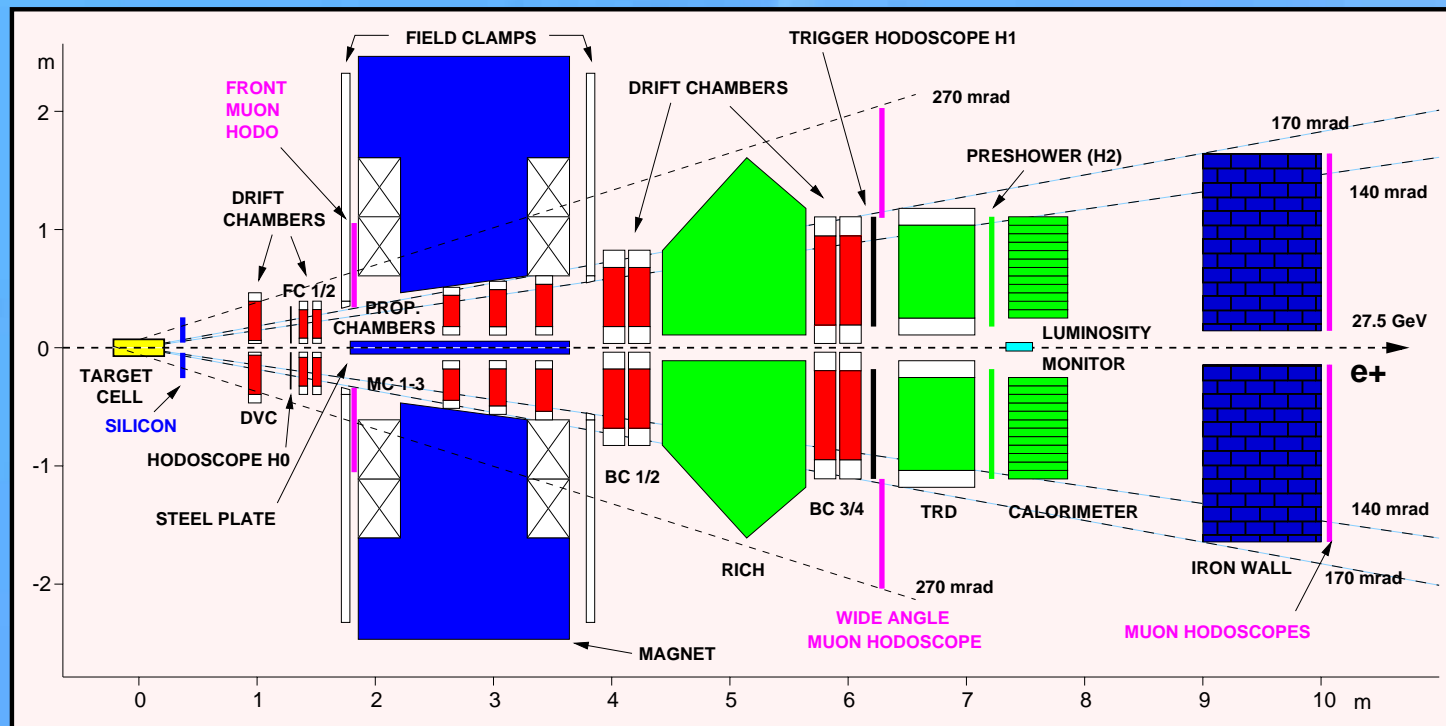
$L_{\mu\nu}$: purely electromagnetic \implies calculable

$$W^{\mu\nu} \sim F_1(x, Q^2) + F_2(x, Q^2) + g_1(x, Q^2) + g_2(x, Q^2)$$

$$\text{(for spin 1)} \quad -b_1(x, Q^2) + \frac{1}{6}b_2(x, Q^2) + \frac{1}{2}b_3(x, Q^2) + \frac{1}{2}b_4(x, Q^2)$$

$F_1, F_2 / g_1, g_2 \implies$ **Unpolarized / Polarized Structure Functions**

The HERMES Detector at DESY



Kinematic Range: $0.02 \leq x \leq 0.8$, $1\text{GeV}^2 \leq Q^2 \leq 15\text{GeV}^2$ at $W \geq 2\text{GeV}$
 $\Theta_x \leq 175 \text{ mrad}$, $40 \text{ mrad} \leq \Theta_y \leq 140 \text{ mrad}$

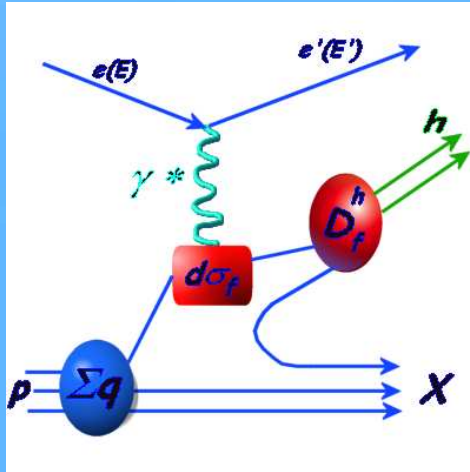
Reconstruction: $\delta p/p$ 1.0 - 2.0%, $\delta\Theta \leq 0.6\text{mrad}$

Internal Gas Target: $\vec{H}e$, \vec{D} , \vec{H} , \mathbf{H}^\uparrow unpol: H_2 , D_2 , He, N_2 , Ne, Ar, Kr, Xe

Particle ID: TRD, Preshower, Calorimeter

\Rightarrow 1997: Čerenkov 1998 \Rightarrow : RICH

Semi-inclusive DIS



Correlation between detected hadron and struck q_f
 \Rightarrow 'Flavor - Separation'

Inclusive DIS: $\Delta\Sigma = \sum_i (\Delta q_i(x) + \Delta \bar{q}_i(x))$

Semi-inclusive DIS: $\Delta u, \Delta \bar{u}, \Delta d, \Delta \bar{d}, \Delta s, \Delta \bar{s}$

In LO-QCD:

$$\begin{aligned}
 A_1^h(\mathbf{x}, Q^2) &= \frac{\sigma_{1/2}^h - \sigma_{3/2}^h}{\sigma_{1/2}^h + \sigma_{3/2}^h} \sim \frac{\sum_f e_f^2 \Delta q_f(\mathbf{x}, Q^2) \int dz D_f^h(z, Q^2)}{\sum_f e_f^2 q_f(\mathbf{x}, Q^2) \int dz D_f^h(z, Q^2)} \\
 &\sim \sum_q \underbrace{\frac{e_q^2 q(x) \int dz D_q^h(z)}{\sum_{q'} e_{q'}^2 q'(x) \int dz D_{q'}^h(z)}}_{P_q^h(\mathbf{x}, z)} \frac{\Delta q(\mathbf{x})}{q(\mathbf{x})}
 \end{aligned}$$

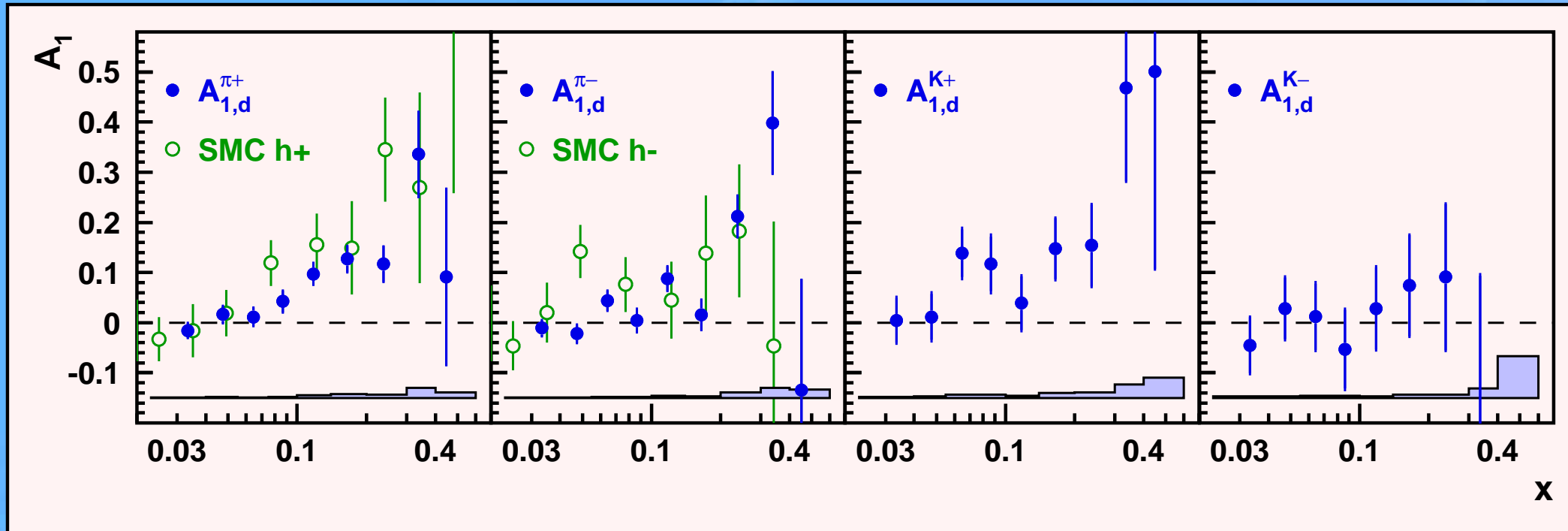
- Solve linear system for \vec{Q} with

$$\tilde{\mathbf{A}} = (\mathbf{A}_{1,p}(\mathbf{x}), \mathbf{A}_{1,d}(\mathbf{x}), \mathbf{A}_{1,p}^{\pi^\pm}(\mathbf{x}), \mathbf{A}_{1,d}^{\pi^\pm}(\mathbf{x}), \mathbf{A}_{1,d}^{\mathbf{K}^\pm}(\mathbf{x}))$$

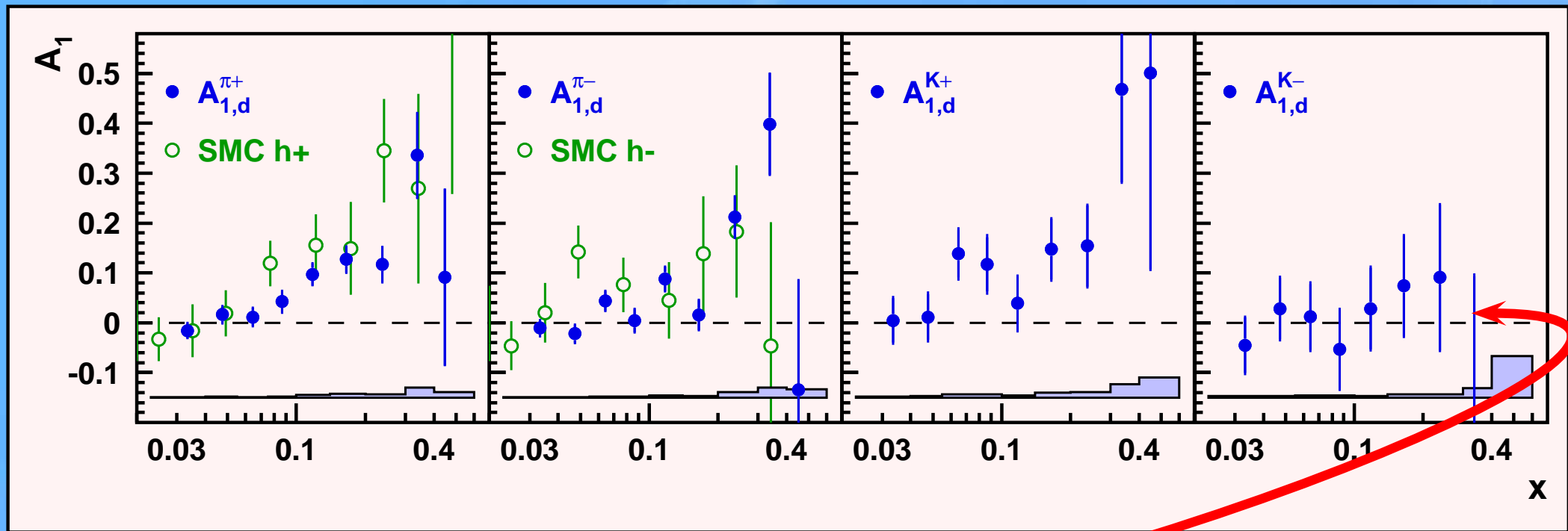
$$\tilde{\mathbf{Q}} = \left(\frac{\Delta u}{u}, \frac{\Delta d}{d}, \frac{\Delta \bar{u}}{\bar{u}}, \frac{\Delta \bar{d}}{\bar{d}}, \frac{\Delta s}{s} \right)$$

$$\tilde{\mathbf{A}} = \mathcal{P} \vec{Q}$$

Hadron Asymmetries on the Deuteron



Hadron Asymmetries on the Deuteron

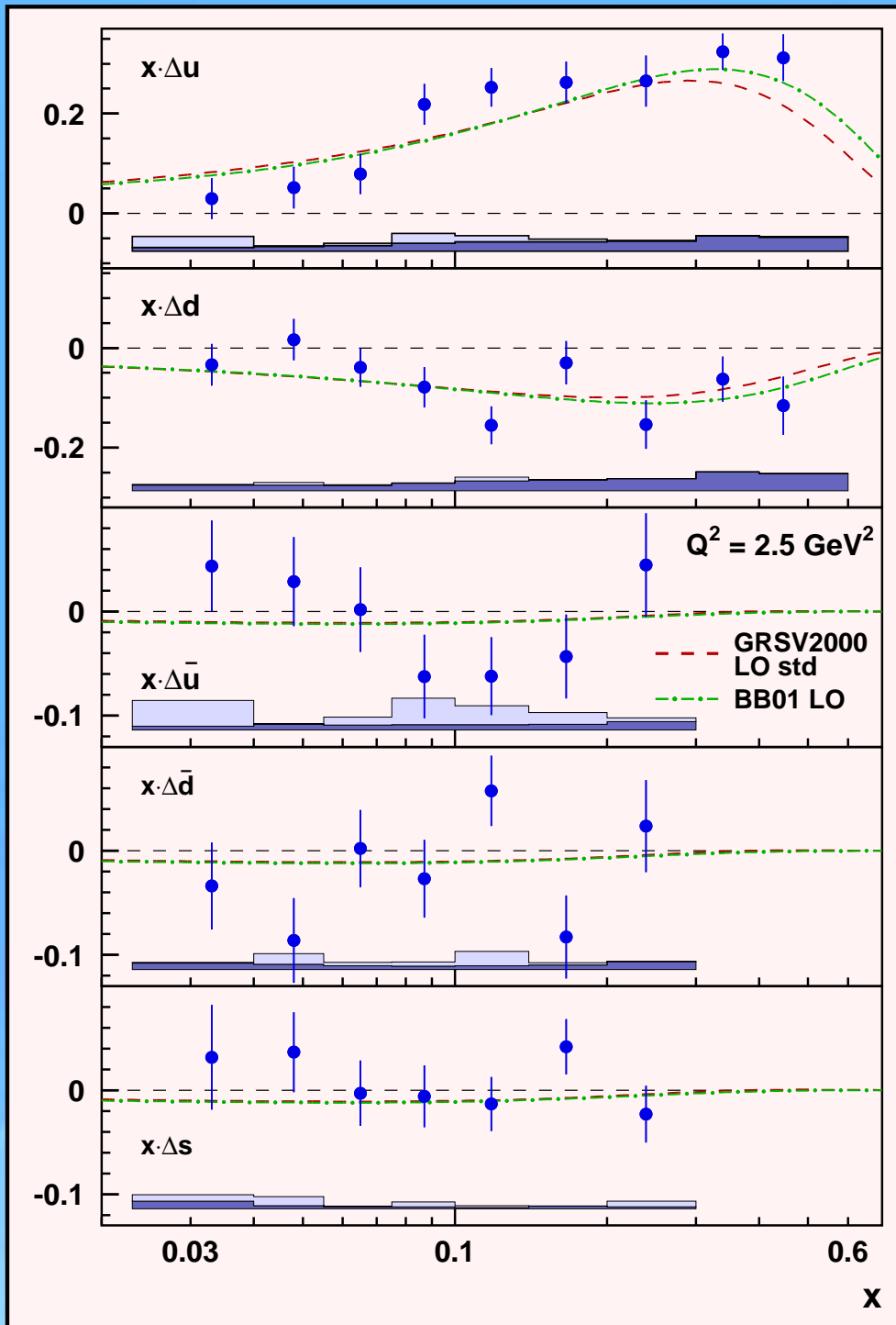


- $A_1^{K^-}(x) \approx 0$!! $\implies K^- = (\bar{u}s)$ is an all-sea object

- statistics sufficient for 5-parameter fit $\tilde{Q} = \left(\frac{\Delta u}{u}, \frac{\Delta d}{d}, \frac{\Delta \bar{u}}{\bar{u}}, \frac{\Delta \bar{d}}{\bar{d}}, \frac{\Delta s}{s} \right)$

Polarized Quark Densities

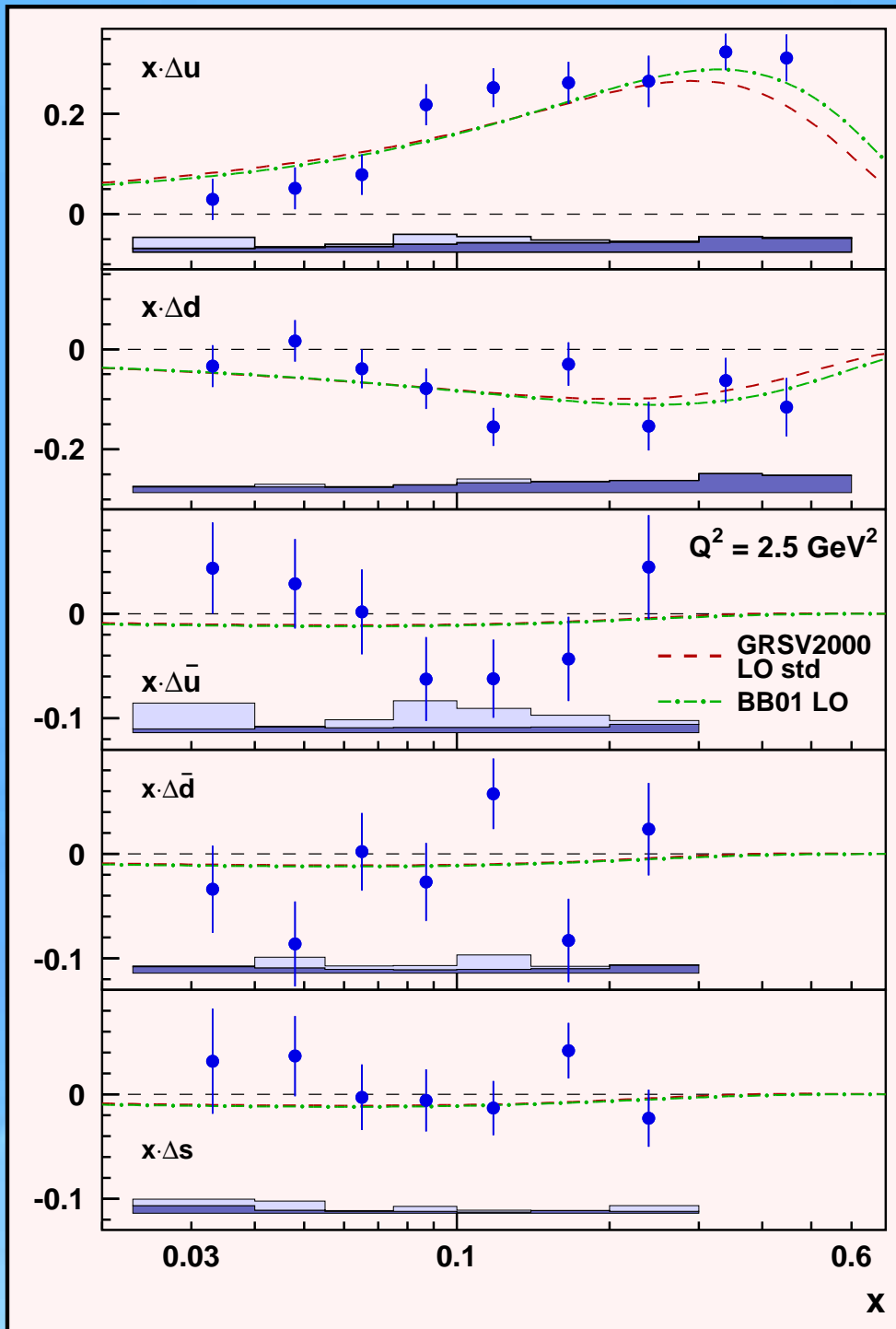
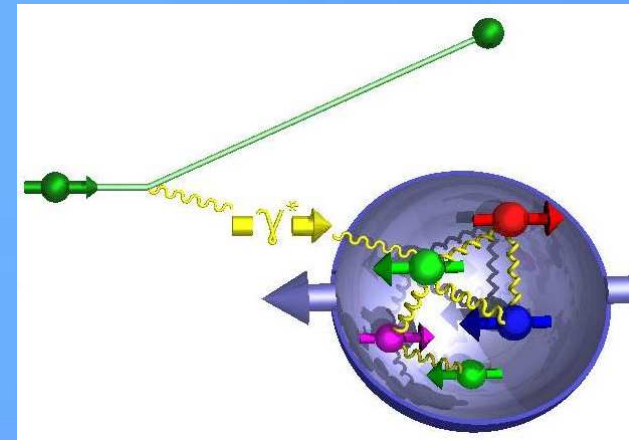
$$\Delta q_f(x) := q_f^+(x) - q_f^-(x)$$



Polarized Quark Densities

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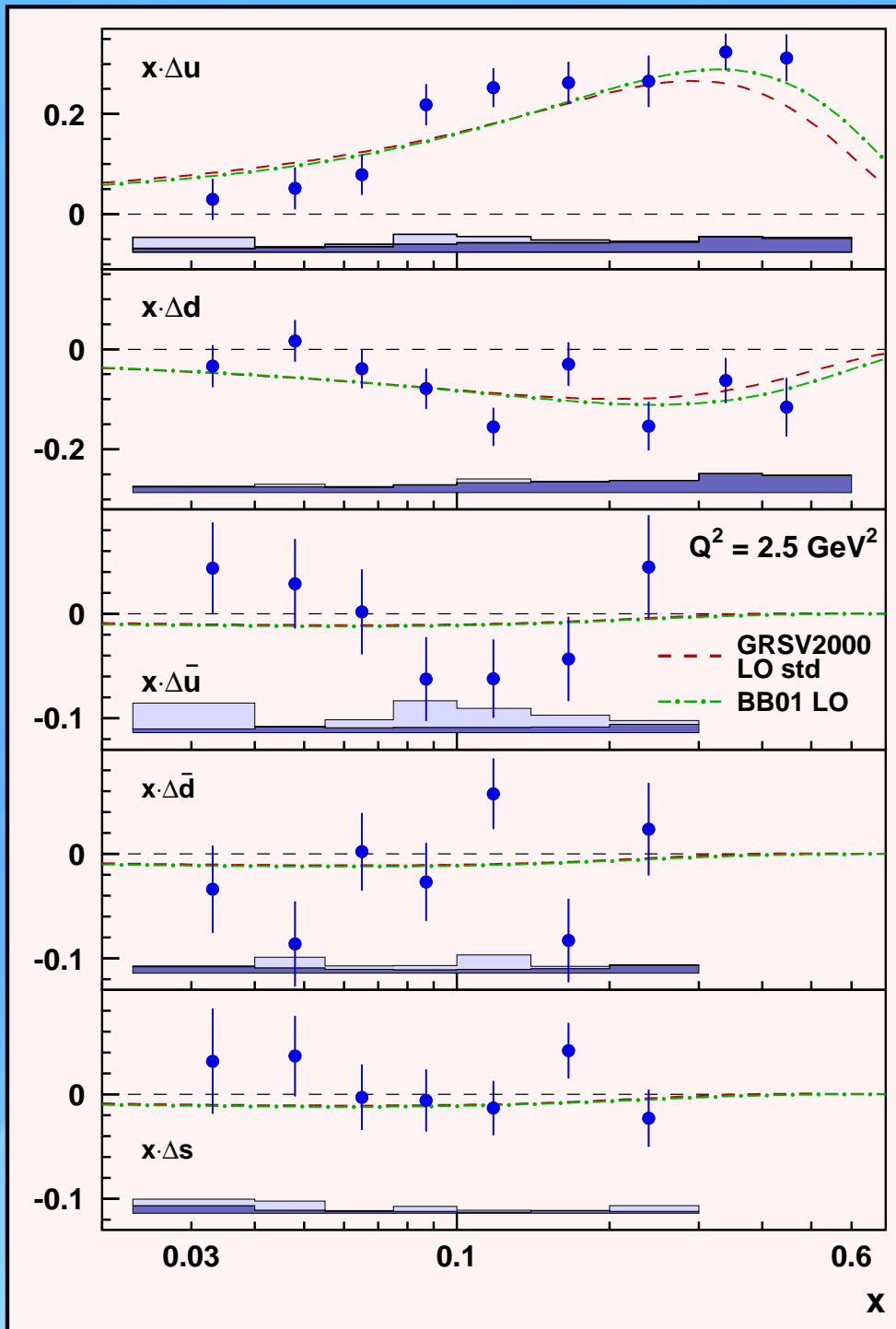
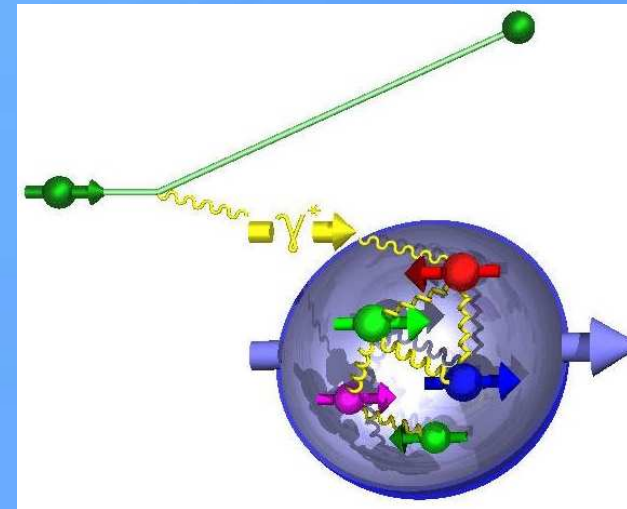
- $\Delta u(x) > 0$
 \Rightarrow polarized parallel to the proton



Polarized Quark Densities

$$\Delta q_f(\mathbf{x}) := q_f^+(\mathbf{x}) - q_f^-(\mathbf{x})$$

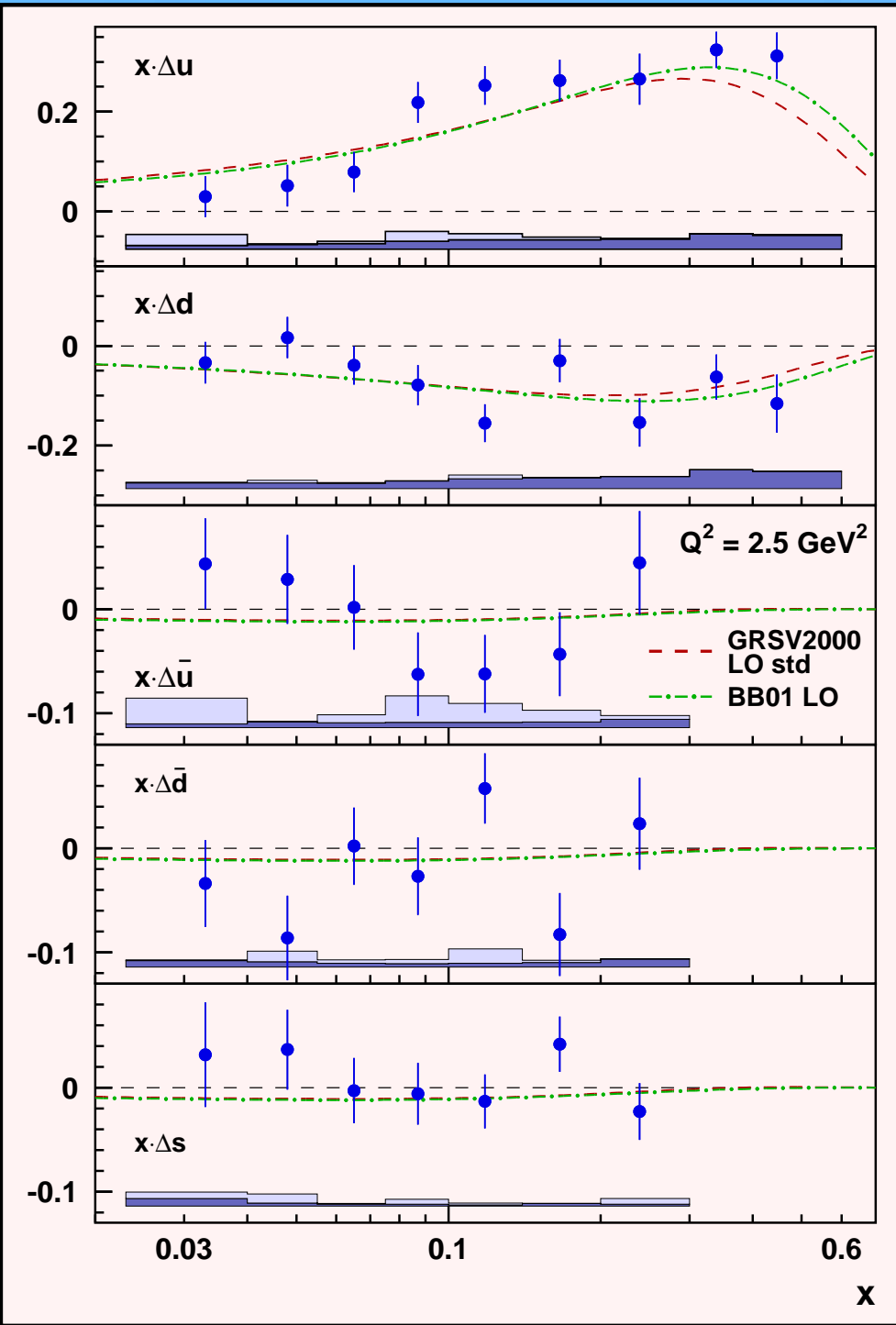
- $\Delta u(\mathbf{x}) > 0$
 \Rightarrow polarized parallel to the proton
- $\Delta d(\mathbf{x}) < 0$
 \Rightarrow polarized anti-parallel to the proton



Polarized Quark Densities

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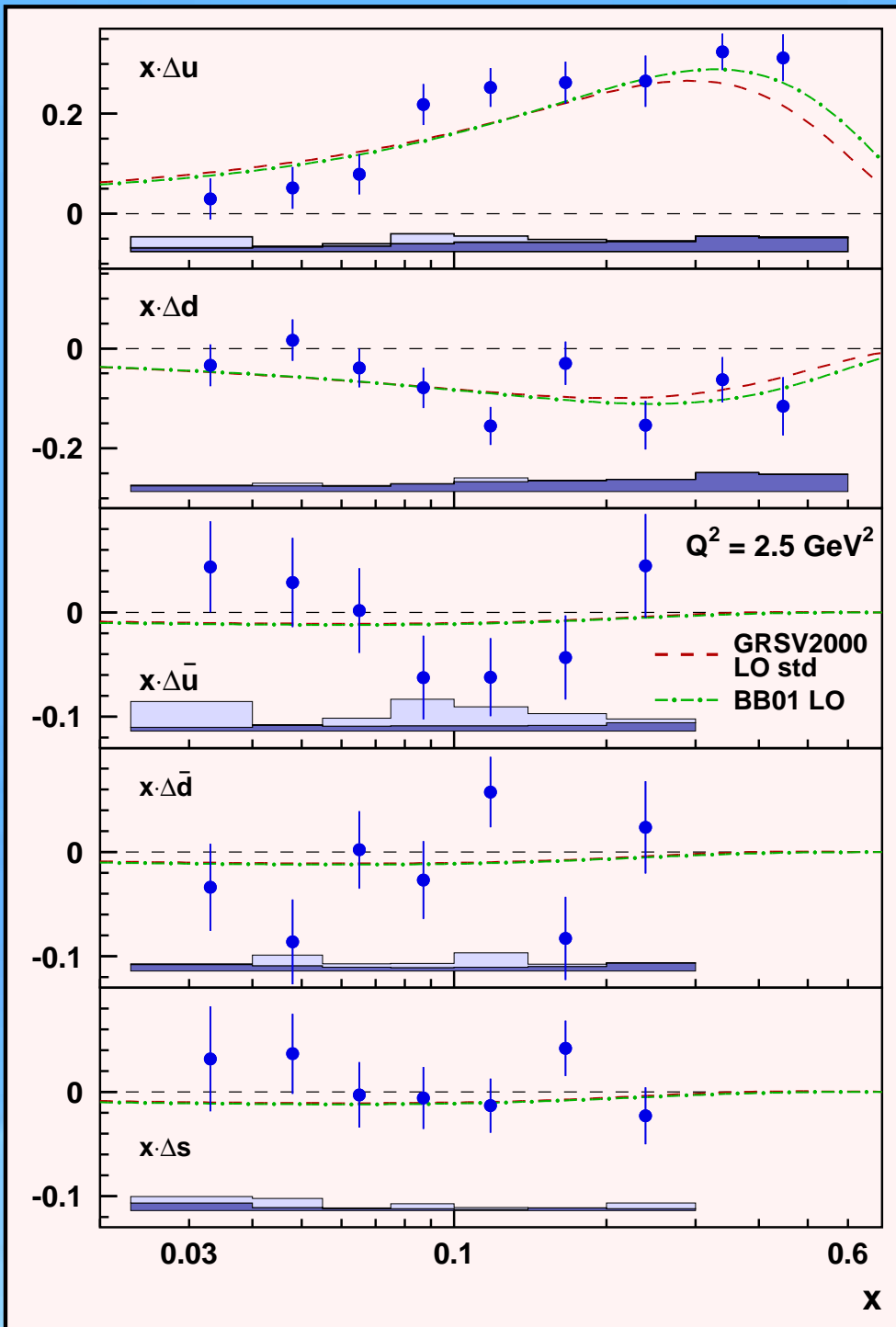
- $\Delta u(x) > 0$
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- $\Delta u(x)$ and $\Delta d(x)$
 good agreement with NLO-QCD fit



Polarized Quark Densities

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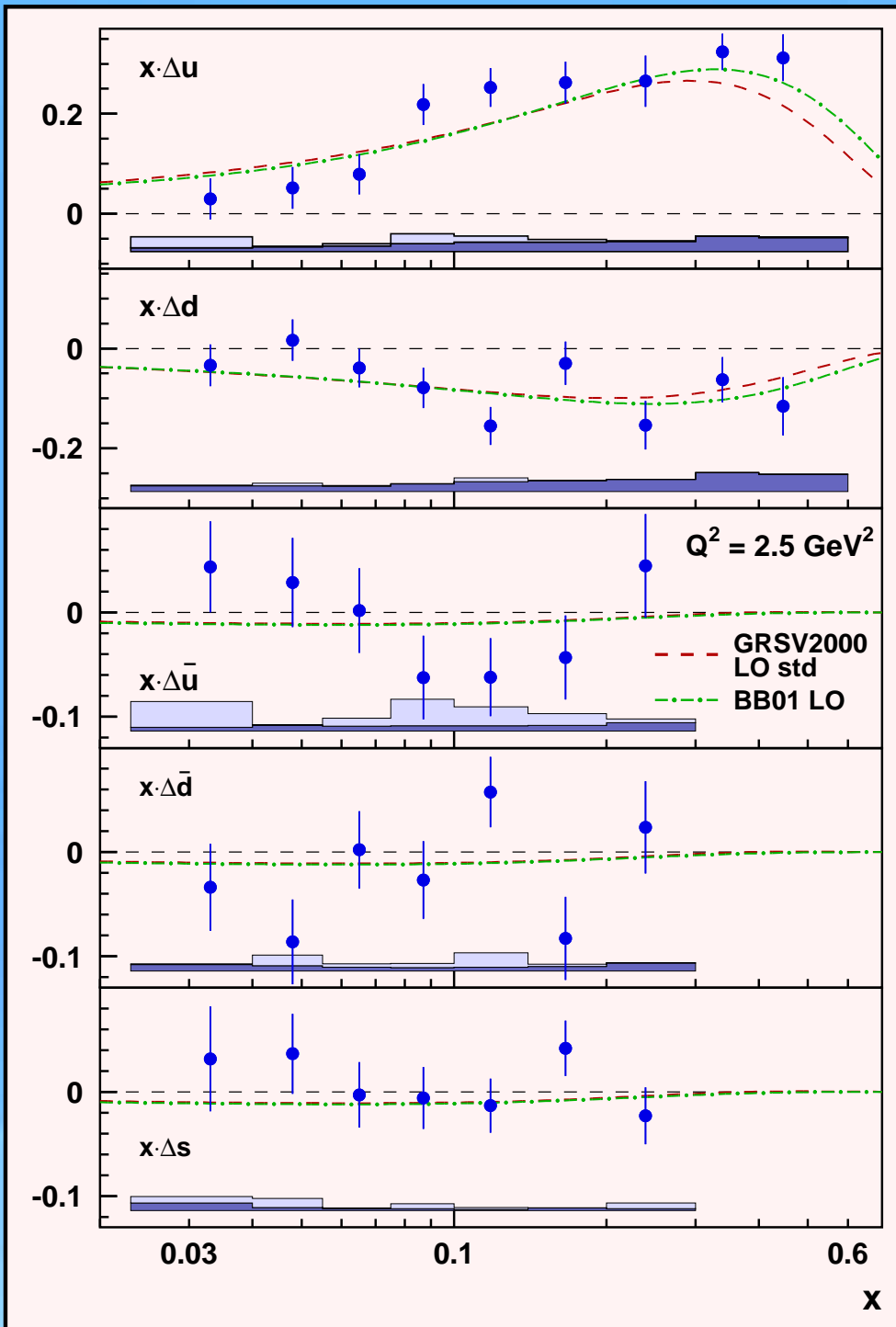
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- $\Delta \bar{u}(x), \Delta \bar{d}(x) \sim 0$



Polarized Quark Densities

$$\Delta q_f(x) := q_f^+(x) - q_f^-(x)$$

- $\Delta u(x) > 0$
 \implies polarized parallel to the proton
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- $\Delta u(x)$ and $\Delta d(x)$
 good agreement with NLO-QCD fit
- $\Delta \bar{u}(x), \Delta \bar{d}(x) \sim 0$
- No indication for $\Delta s(x) < 0$



Access to Transversity

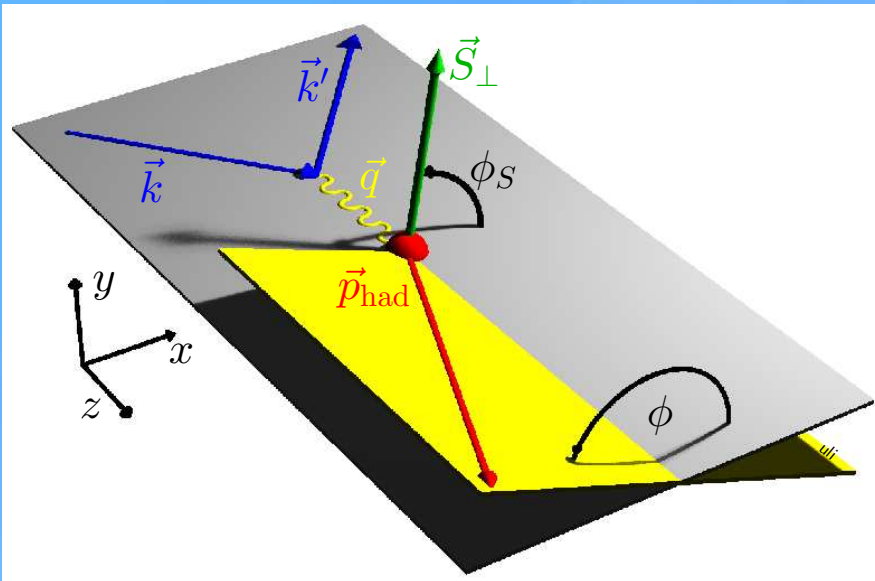
Single spin azimuthal asymmetries on a transverse polarized Target

$$ep^{\uparrow} \longrightarrow e'\pi X$$

$$\sigma^{ep \rightarrow e\pi X} = \sum_q f^{N \rightarrow q} \otimes \sigma^{eq \rightarrow eq} \otimes D^{q \rightarrow \pi}$$

**Distribution-
function**
 h_1

**Fragmentat.-
function**
 H_1^{\perp} (Collins)

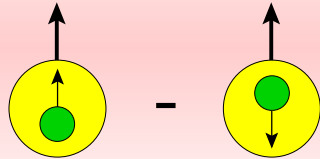


$$A_{\text{UT}}^{\text{h}}(\phi, \phi_s) = \frac{1}{|\mathbf{S}_{\text{T}}|} \frac{N_{\text{h}}^{\uparrow}(\phi, \phi_s) - N_{\text{h}}^{\downarrow}(\phi, \phi_s)}{N_{\text{h}}^{\uparrow}(\phi, \phi_s) + N_{\text{h}}^{\downarrow}(\phi, \phi_s)}$$

$$A_{\text{UT}}^{\text{Collins}} \propto \frac{\sum_q e_q^2 \delta q(\mathbf{x}) H_1^{\perp, q}(\mathbf{z})}{\sum_q e_q^2 q(\mathbf{x}) D_1^q(\mathbf{z})}$$

Transversely Polarized Target

Transversity $h_1(x)$

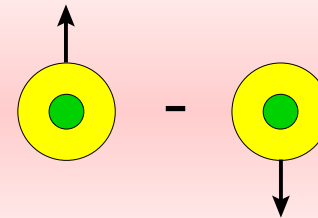


T-even

χ -odd

combined with χ -odd
fragmentation function $H_1^\perp(z)$
(Collins function)

Sivers function $f_{1T}^\perp(x)$



“naïve T-odd”

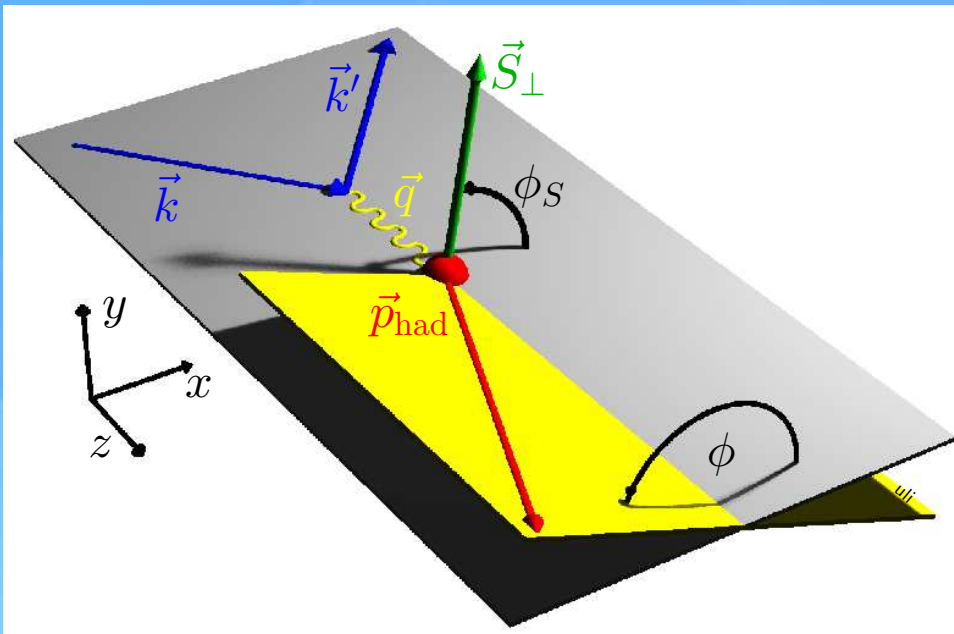
χ -even

$\neq 0$ indicates
non-vanishing orbital angular
momentum of quarks

Azimuthal Asymmetries

Measurement of cross section asymmetries depending on the azimuthal angles ϕ and ϕ_S

$$\mathbf{A}(\phi, \phi_S) = \frac{1}{S_{\perp}} \frac{\mathbf{N}^{\uparrow}(\phi, \phi_S) - \mathbf{N}^{\downarrow}(\phi, \phi_S)}{\mathbf{N}^{\uparrow}(\phi, \phi_S) + \mathbf{N}^{\downarrow}(\phi, \phi_S)}$$



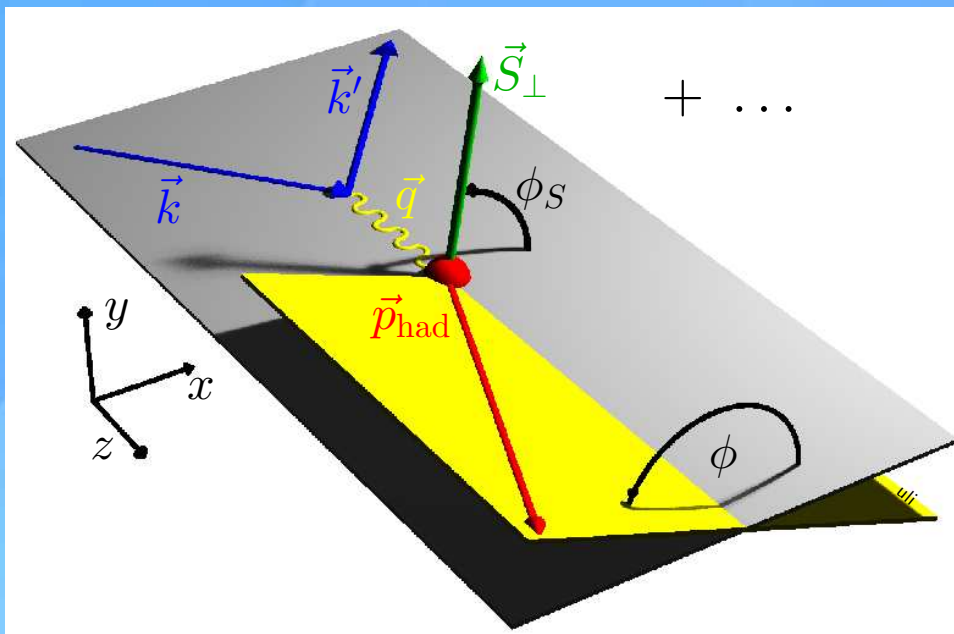
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$$\sim \dots \sin(\phi + \phi_S) \sum_{\mathbf{q}} \mathbf{e}_{\mathbf{q}}^2 \cdot \mathcal{I} \left[\dots \mathbf{h}_1^{\mathbf{q}}(\mathbf{x}, \vec{\mathbf{p}}_{\mathbf{T}}^2) \cdot \mathbf{H}_1^{\perp \mathbf{q}}(z, \vec{\mathbf{k}}_{\mathbf{T}}^2) \right]$$

$$+ \dots \sin(\phi - \phi_S) \sum_{\mathbf{q}} \mathbf{e}_{\mathbf{q}}^2 \cdot \mathcal{I} \left[\dots \mathbf{f}_{1\mathbf{T}}^{\perp \mathbf{q}}(\mathbf{x}, \vec{\mathbf{p}}_{\mathbf{T}}^2) \cdot \mathbf{D}_1^{\mathbf{q}}(z, \vec{\mathbf{k}}_{\mathbf{T}}^2) \right]$$



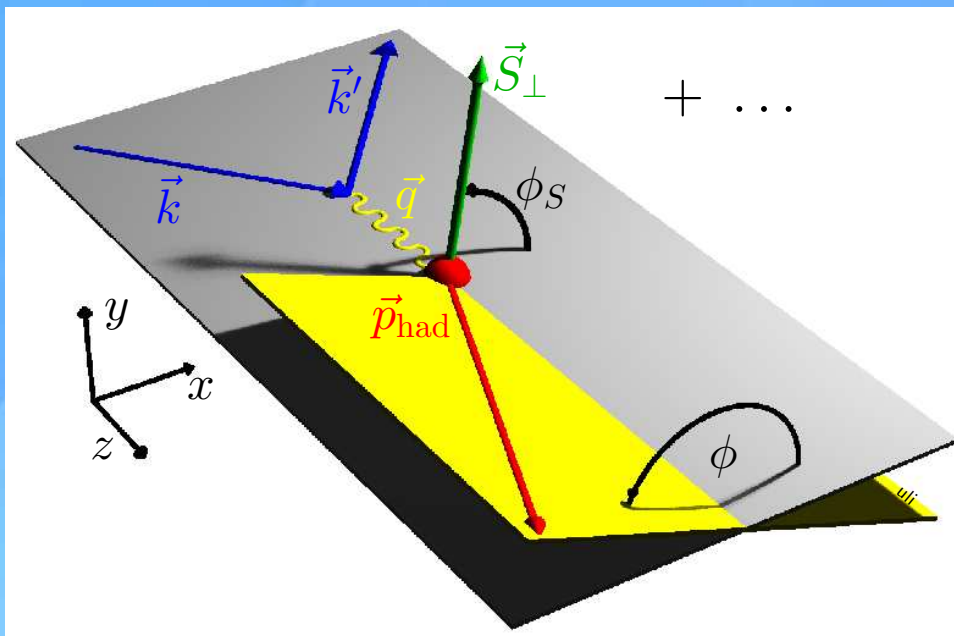
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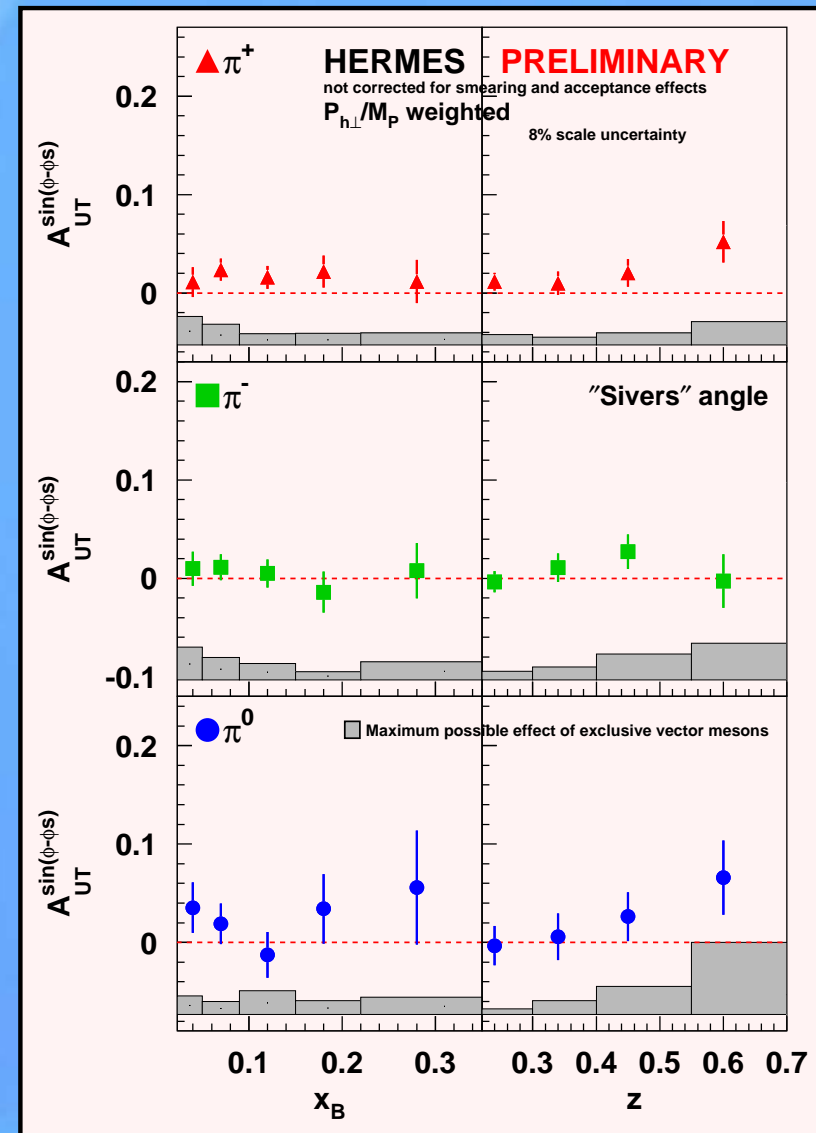
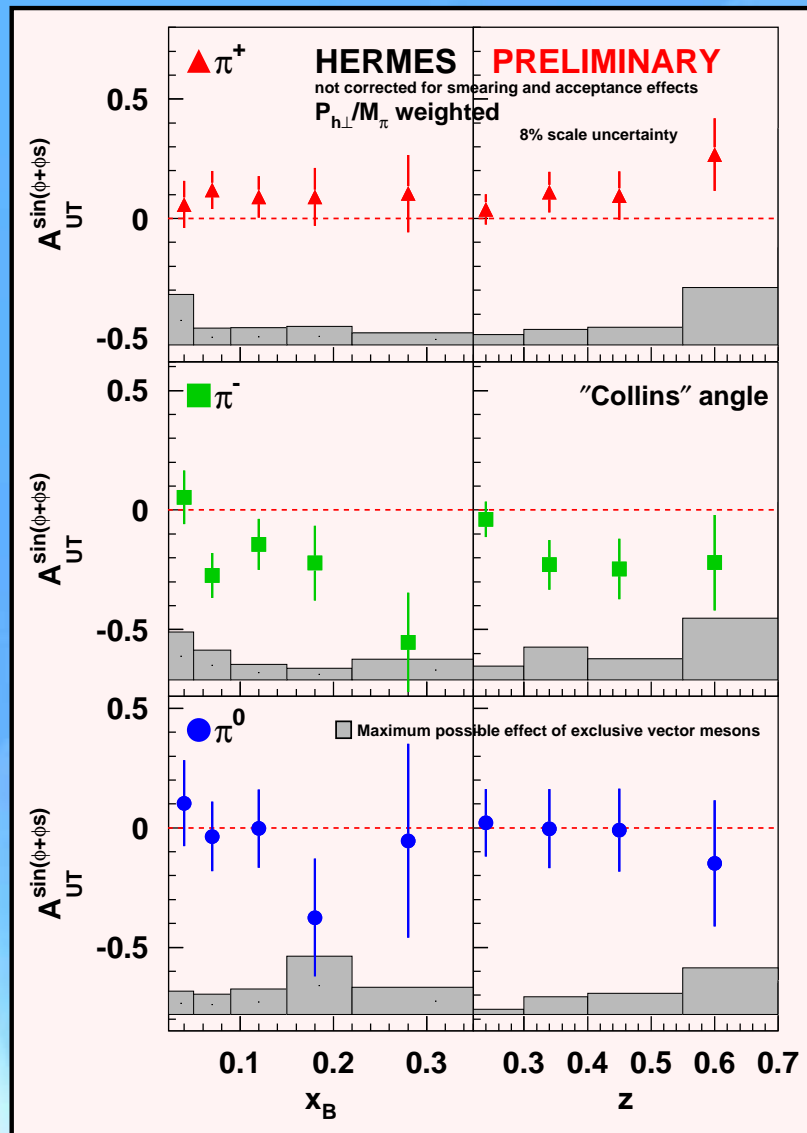


$\mathcal{I}[\dots]$: convolution integral over initial ($\vec{\mathbf{p}}_{\mathbf{T}}$) and final ($\vec{\mathbf{k}}_{\mathbf{T}}$) quark transverse momenta

$P_{h\perp}$ Weighted Asymmetries

$$A^{\sin(\phi+\phi_S)} \sim h_1(\mathbf{x}) \cdot \mathbf{H}_1^{\perp(1)}(z)$$

$$A^{\sin(\phi-\phi_S)} \sim f_{1T}^{\perp(1)}(\mathbf{x}) \cdot \mathbf{D}_1(z)$$



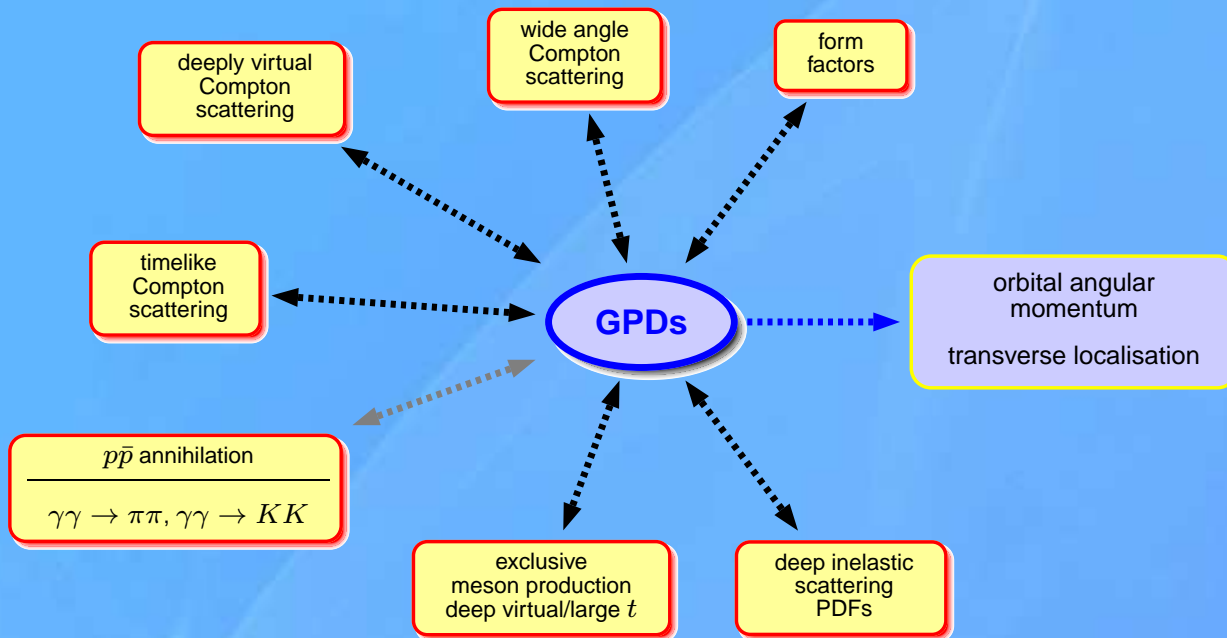
The Hermes Quest for L_q

Study of hard **exclusive processes** leads to a new class of PDFs

Generalised Parton Distributions

$$H^q, E^q, \tilde{H}^q, \tilde{E}^q$$

⇒ possible access to orbital angular momentum

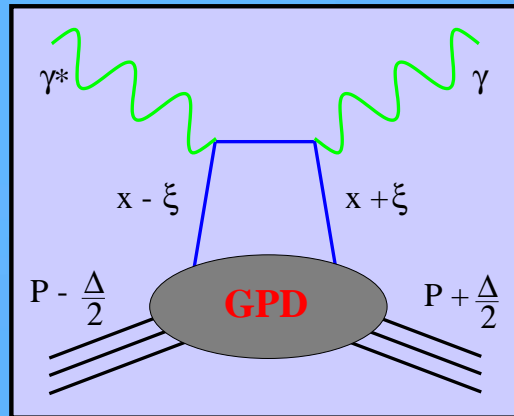


$$J_q = \frac{1}{2} \left(\int_{-1}^1 x dx (H^q + E^q) \right)_{t \rightarrow 0}$$

$$J_q = \frac{1}{2} \Delta \Sigma + L_q$$

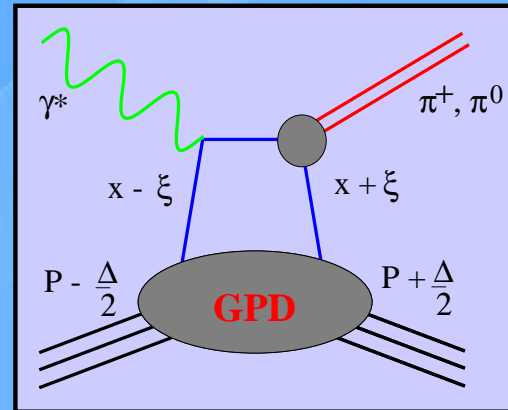
exclusive: all products of a reaction are detected
 ⇒ missing energy (ΔE) and missing Mass (M_x) = 0

quantum numbers of final state \Rightarrow select different GPDs



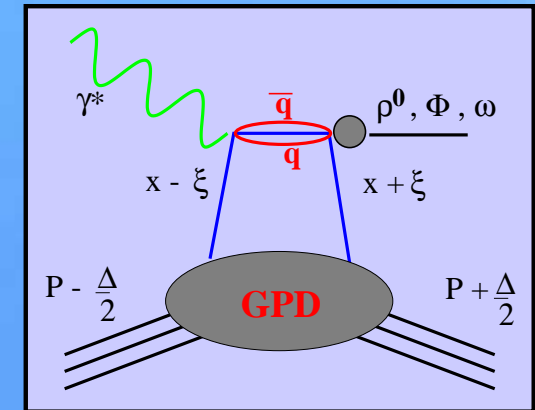
DVCS:

$$H^q, E^q, \tilde{H}^q, \tilde{E}^q$$



pseudo-scalar mesons

$$\tilde{H}^q, \tilde{E}^q$$



vector mesons

$$H^q, E^q$$

What does GPDs characterize?

unpolarized

$$H^q(x, \xi, t)$$

$$E^q(x, \xi, t)$$

polarized

$$\tilde{H}^q(x, \xi, t)$$

$$\tilde{E}^q(x, \xi, t)$$

conserve nucleon helicity

$$H^q(x, 0, 0) = q, \tilde{H}^q(x, 0, 0) = \Delta q$$

flip nucleon helicity

not accessible in DIS

How to Measure GPDs ?

meson production $\rightarrow \sigma_L$

@ Hermes kinematics:

	vector mesons		pseudoscalar mesons	
	σ_L	A_{UT} (nominator)	σ_L	A_{UT} (nominator)
H	$(1 - \xi^2)$	$\sqrt{1 - \xi^2}$		
\tilde{H}			$(1 - \xi^2)$	$\sqrt{1 - \xi^2} \cdot \xi$
E	$(\xi^2 + \frac{t}{4M^2})$	$\sqrt{1 - \xi^2}$		
\tilde{E}			$\xi^2 \frac{t}{4m^2}$	$\sqrt{1 - \xi^2} \cdot \xi$

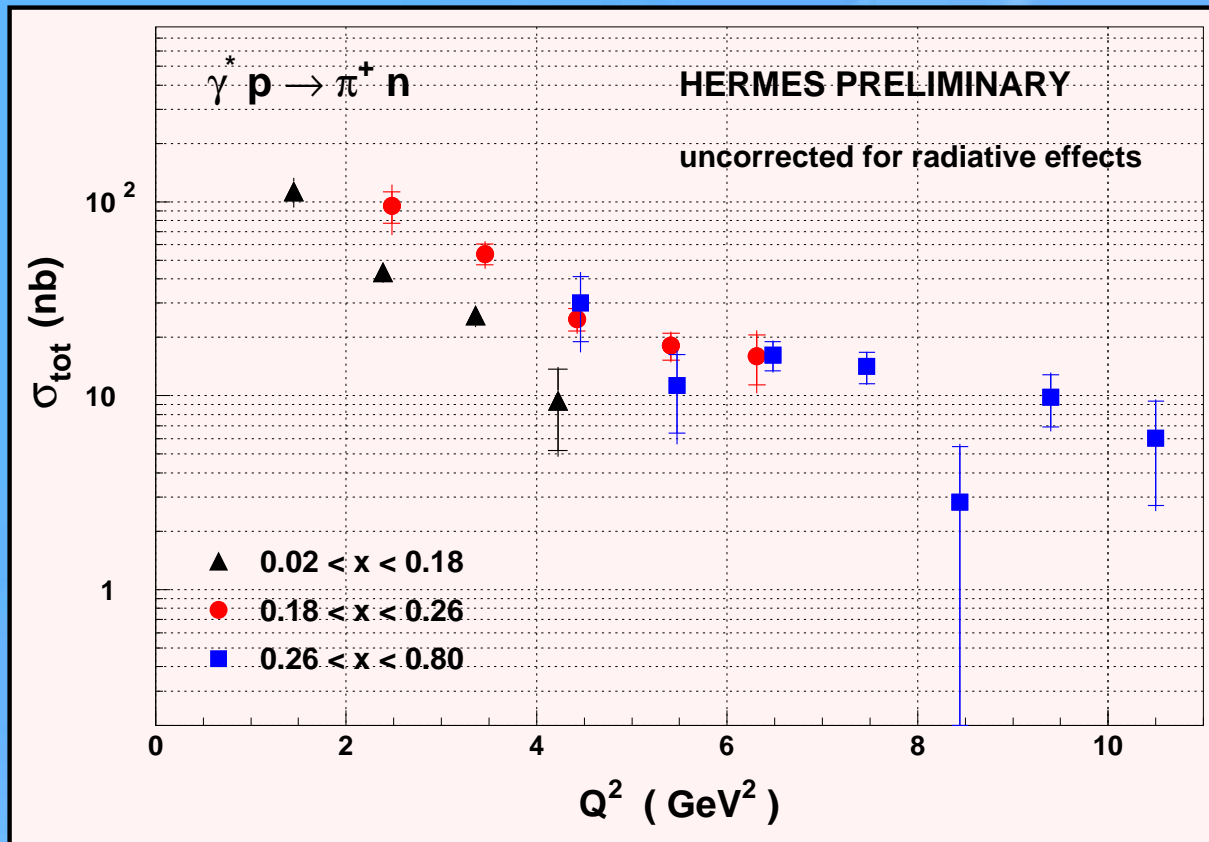
$$\xi \approx \frac{x_B}{2 - x_B}$$

$$\xi \approx 0.01 - 0.3$$

$$\xi|_{x=0.1} \approx 0.05$$

$$\frac{t}{4M^2} \approx 0.02 - 0.1$$

Exclusive π^+ result



- complete new data
- cross section in 3 x-bins
- sensitivity to \tilde{E} at higher x
- absolute normalization of GPDs

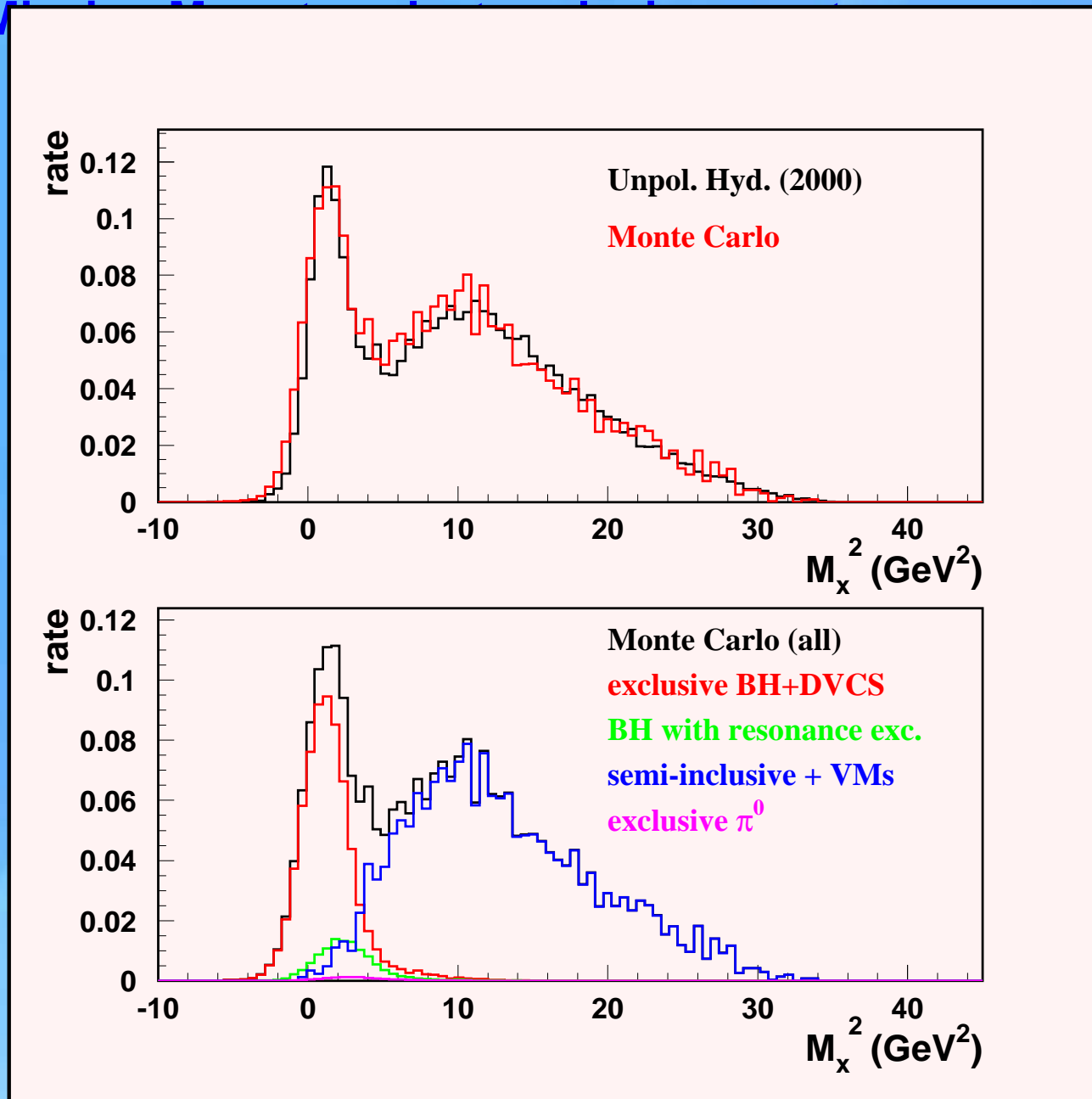
How to Measure GPDs ?

	DVCS		
	A_C, A_{LU}	A_{UL}	A_{UT}
	(twist-2 amplitudes of the interference terms only)		
H	F_1	$\xi(F_1 + F_2)$	$\xi^2 F_1 + \frac{t}{4M^2}(1 - \xi^2)F_2$
\tilde{H}	$\xi(F_1 + F_2)$	F_1	$\xi^2(F_1 + F_2)$
E	$\frac{t}{4M^2}F_2$	$\frac{\xi^2}{1+\xi}(F_1 + F_2)$	$\xi^2 F_1 + \frac{t}{4M^2}(F_1 + \xi^2 F_2)$
\tilde{E}		$\frac{\xi^2}{1+\xi}F_1 + \xi \frac{t}{4M^2}F_2$	$\xi^2 \frac{t}{4M^2}(F_1 + F_2)$

F_1 and F_2 ...Dirac and Pauli form factor

\Rightarrow to access E transverse target polarisation is essential

DVCS - Exclusive Scattering

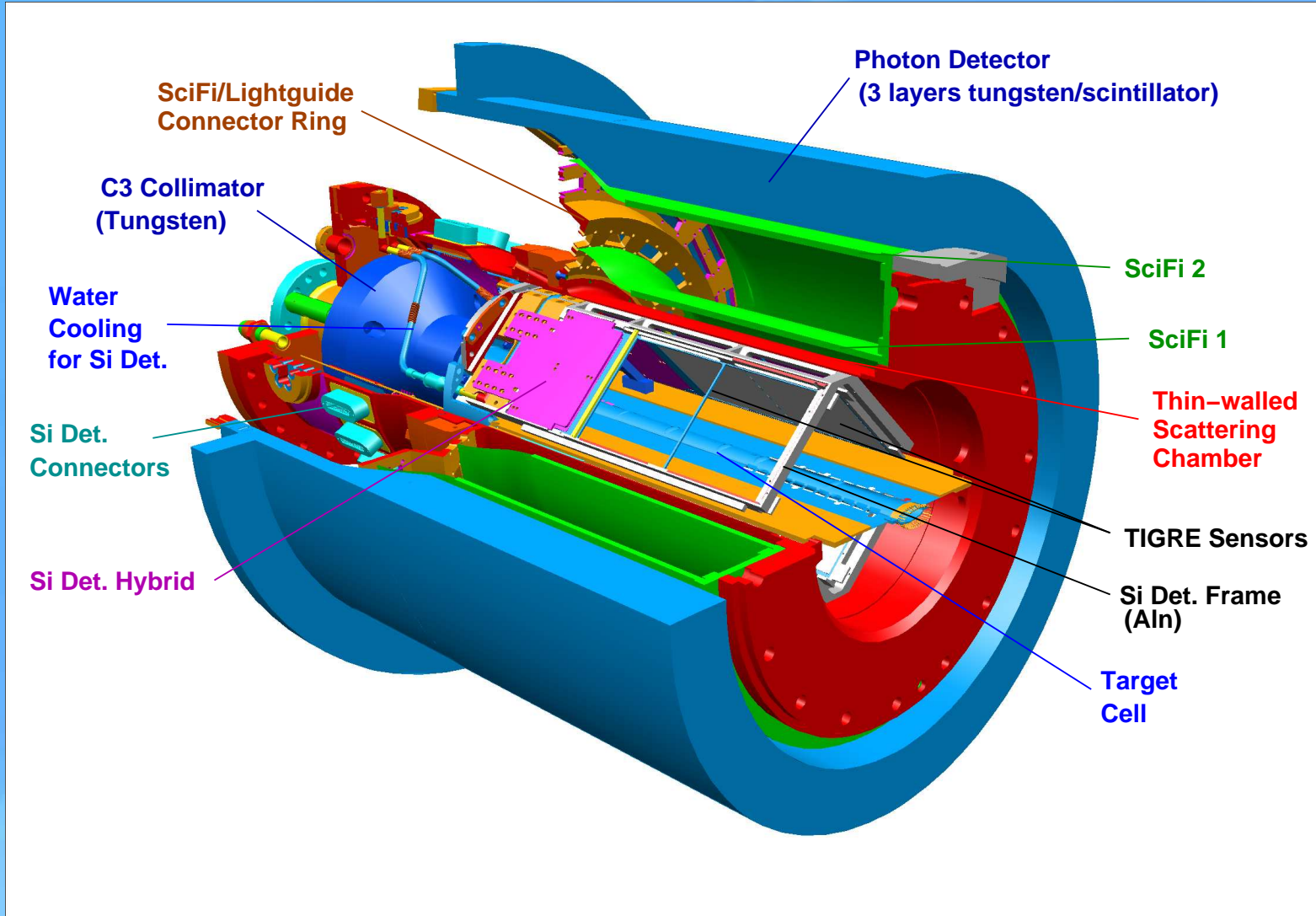


Background from

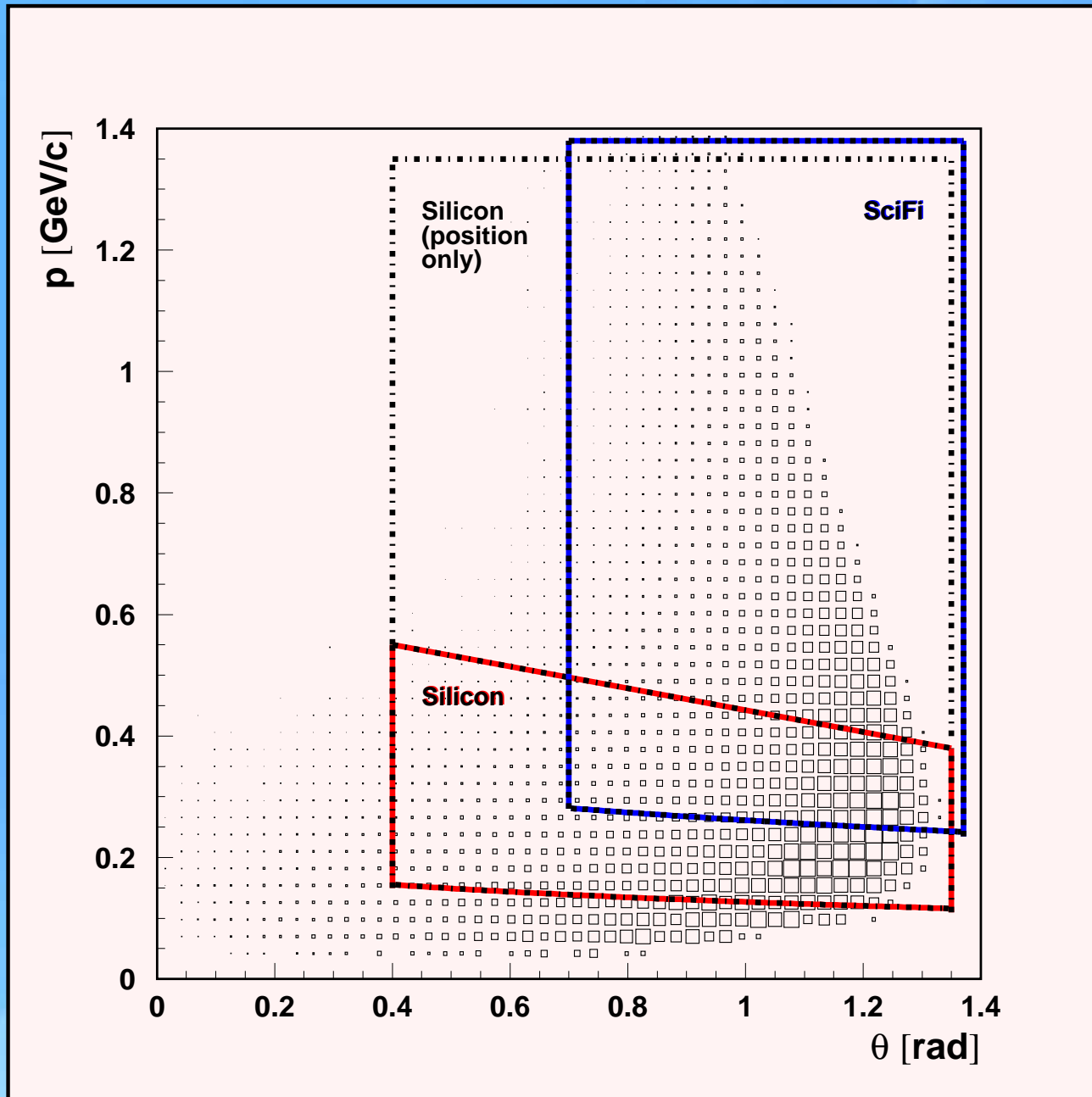
- Resonances
- SIDIS

⇒ tag recoil Nucleon

Measure the recoiling target nucleon



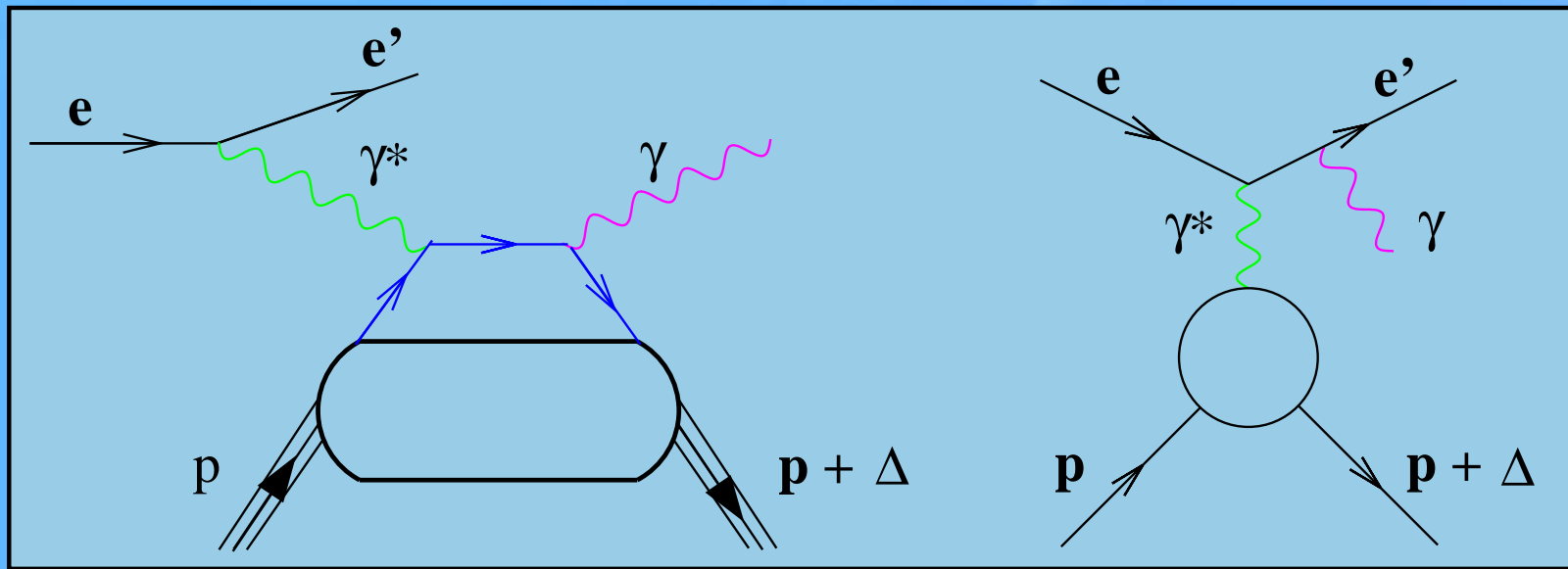
Recoil Detector



- 135 to 1400 MeV/c momentum coverage
- low p cut off due to E-loss in target cell
- 76% acceptance in ϕ
- π - p separation via dE/dx
- Installation summer 2005
- DVCS with with e^- and e^+ beams

- PID essential for flavor decomposition
- Transverse polarized hydrogen data suggest Collins and Sivers
- GPDs give access to orbital angular momentum of quarks
- transverse pol. target needed to access E
- exclusive π production access to \tilde{H}, \tilde{E}
- DVCS access to H
- install the Recoil Detector in summer 2005
- focus on DVCS with e- and e+ beam

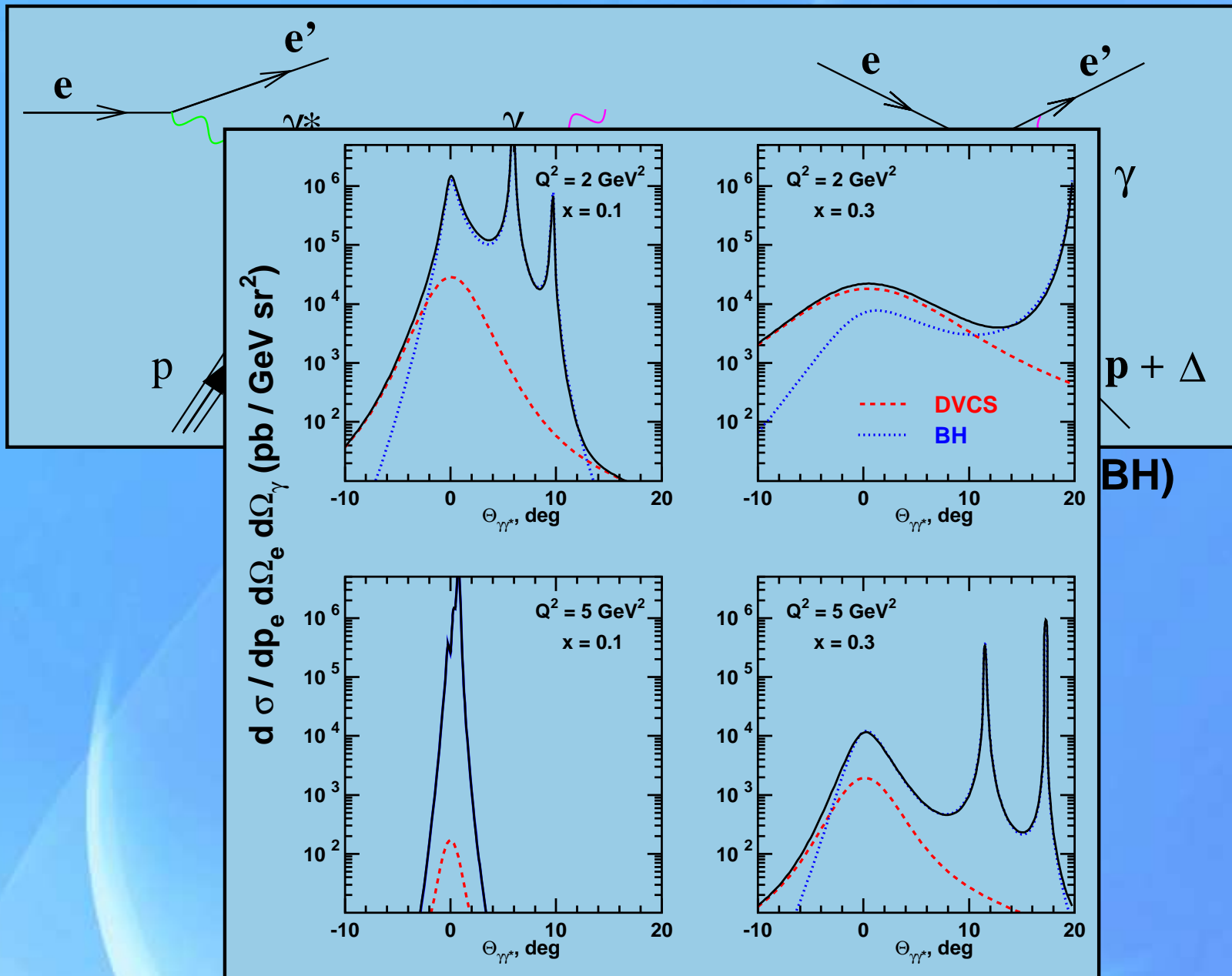
DVCS $\gamma^* p \rightarrow \gamma p$

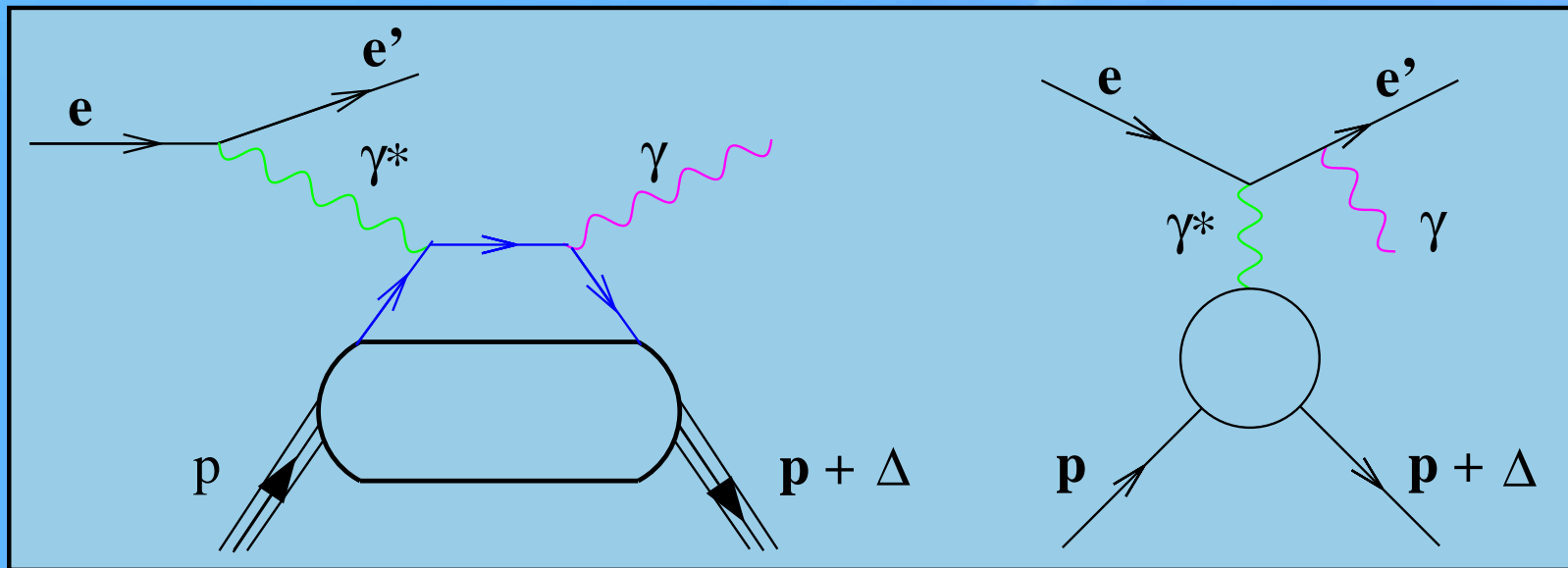


DVCS

Bethe-Heitler (BH)

DVCS $\gamma^* p \rightarrow \gamma p$





DVCS

Bethe-Heitler (BH)

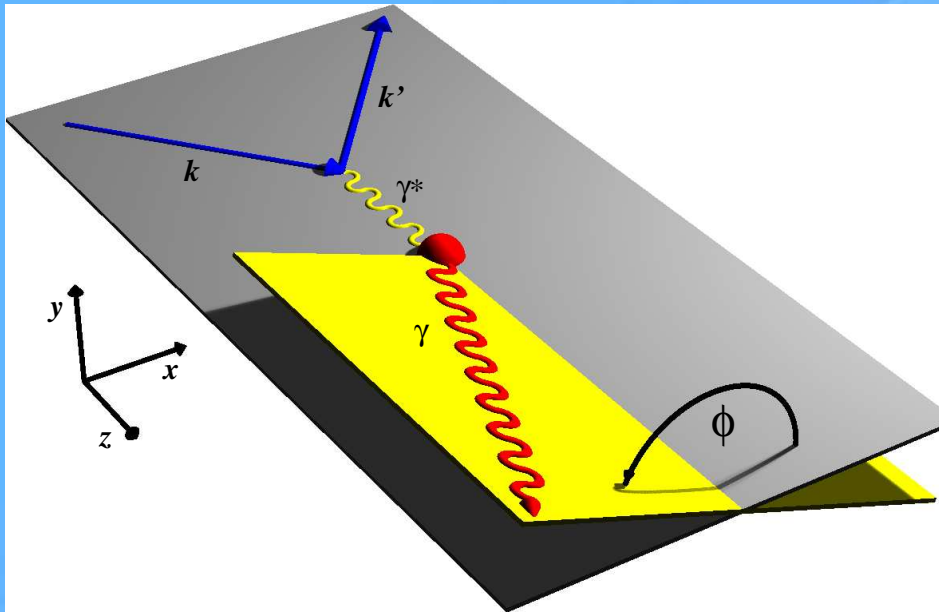
$$d\sigma \propto |\mathcal{T}_{BH} + \mathcal{T}_{DVCS}|^2 =$$

$$|\mathcal{T}_{BH}|^2 + |\mathcal{T}_{DVCS}|^2$$

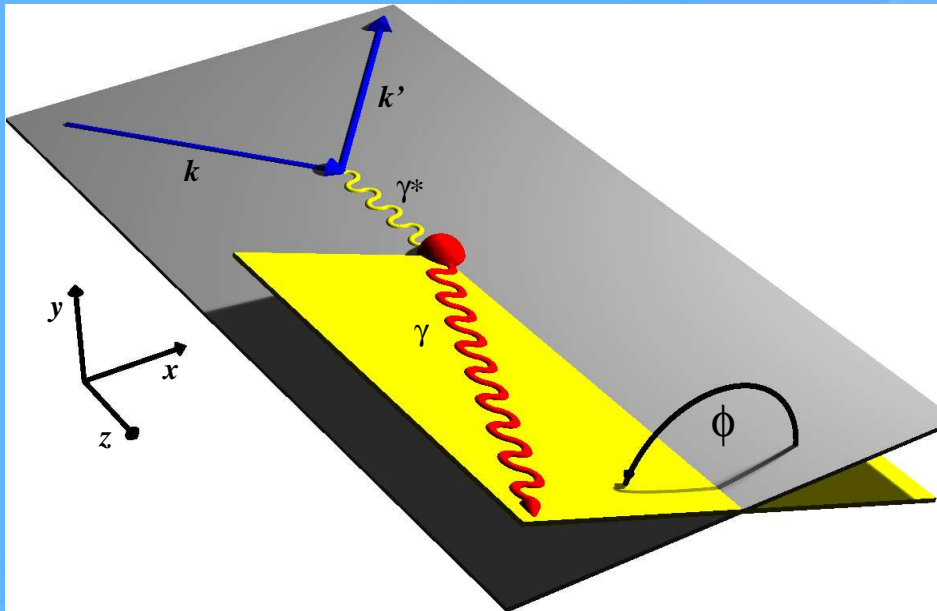
$$+ (\mathcal{T}_{BH}^* \mathcal{T}_{DVCS} + \mathcal{T}_{DVCS}^* \mathcal{T}_{BH})$$

⇒ **Interference term a tool to study DVCS**
exploit azimuthal cross section asymmetries

DVCS Azimuthal Asymmetries



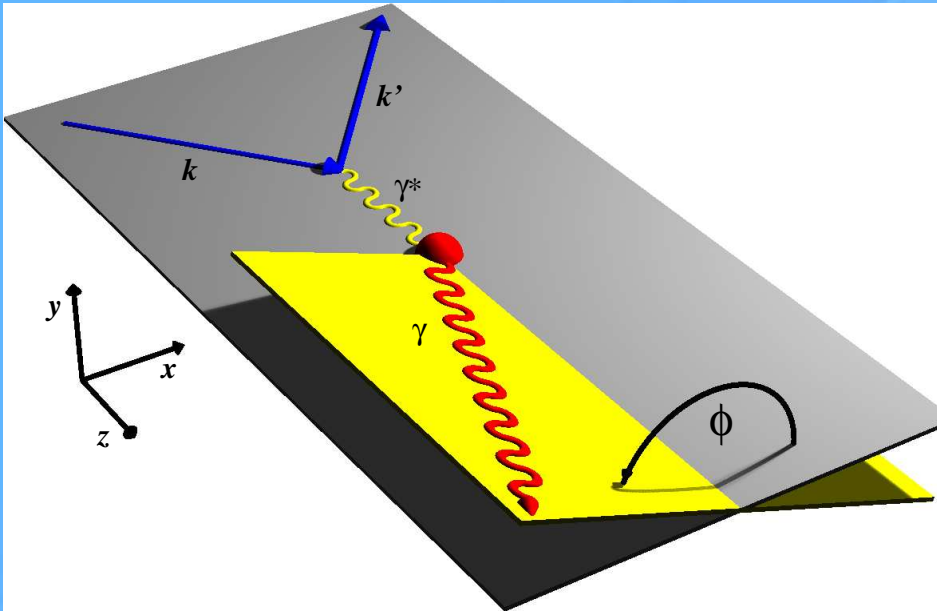
DVCS Azimuthal Asymmetries



Beam Helicity Asymmetry \propto
Imaginary Part

$$\begin{aligned} d\sigma_{\vec{e}^+} - d\sigma_{\leftarrow\vec{e}^+} &\propto \text{Im}(\mathcal{T}_{BH}\mathcal{T}_{DVCS}) \\ &\propto \sin\phi \implies H^q(x, \xi, t) \end{aligned}$$

DVCS Azimuthal Asymmetries



Beam Helicity Asymmetry \propto
Imaginary Part

$$\begin{aligned} d\sigma_{\vec{e}^+} - d\sigma_{\vec{e}^-} &\propto \text{Im}(\mathcal{T}_{BH}\mathcal{T}_{DVCS}) \\ &\propto \sin\phi \implies H^q(x, \xi, t) \end{aligned}$$

Beam Charge Asymmetry \propto
Imaginary Part

$$\begin{aligned} d\sigma_{e^+} - d\sigma_{e^-} &\propto \text{Re}(\mathcal{T}_{BH}\mathcal{T}_{DVCS}) \\ &\propto \cos\phi \implies H^q(x, \xi, t) \end{aligned}$$

e^+ and e^- beams unique to HERA